

# Optimization in industrial contexts in a nutshell !!!

SMAI MODE, March 2016

**Airbus Group Innovations, Applied Mathematics & Simulation department**

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Prepared with *Vassili SRITHAMMAVANH, Régis LEBRUN, Lionel FINE, Matthieu MEAUX, Nabil RACHDI*

**AIRBUS**  
GROUP

# Key Challenges to make Numerical Optimization an Industrial Success at Global Company Level

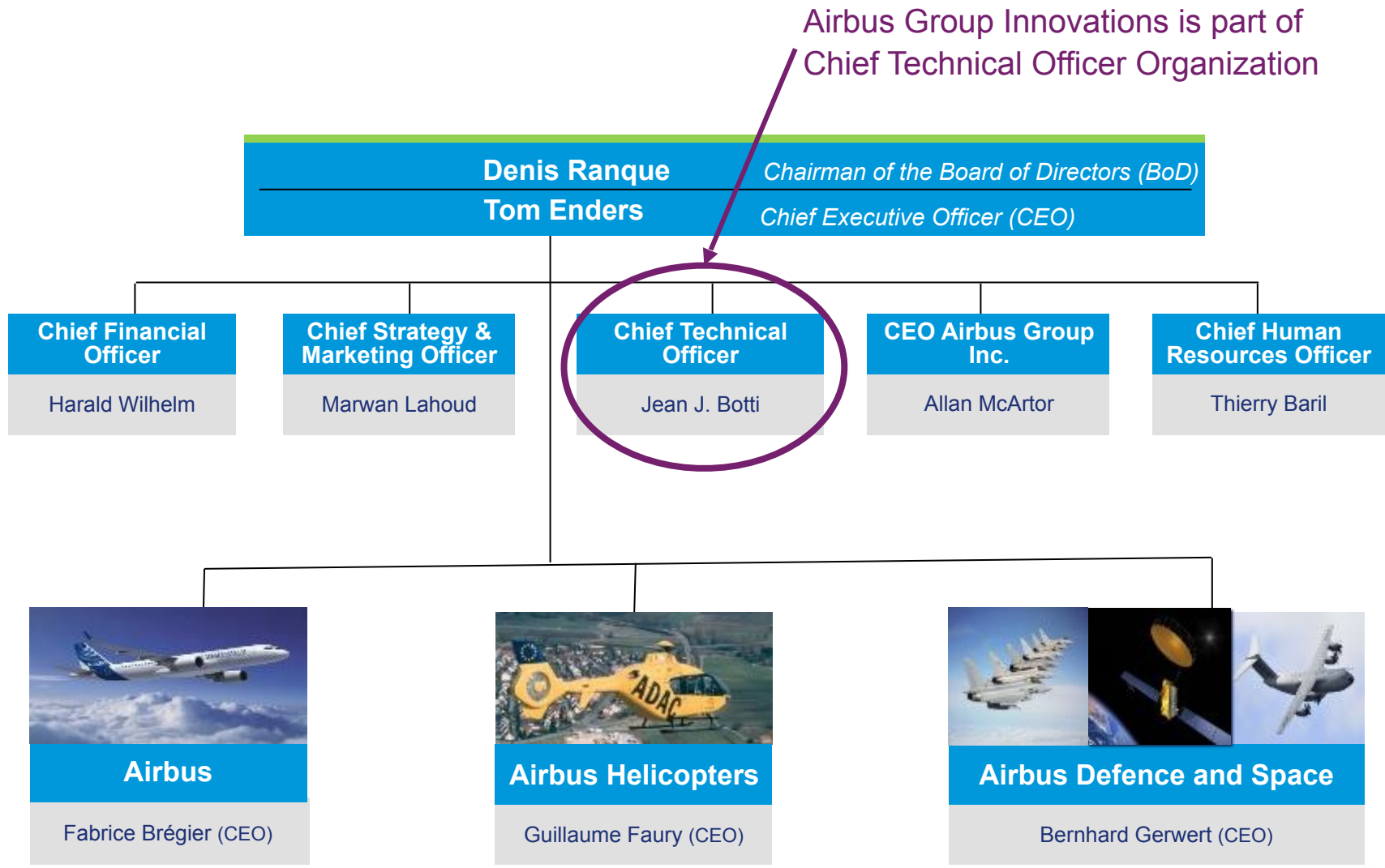


## Outline

- « DIGITALIZATION » applied in aeronautics
- « INNOVATION » at stake and link with numerical optimization activities
- « RESEARCH »: Focus on a research activities
- « FUTURE »: Perspectives

- 1. 3 Divisions & Corporate targets to align
- 2. Size, time-to-market, competitors

# Airbus Group Management structure

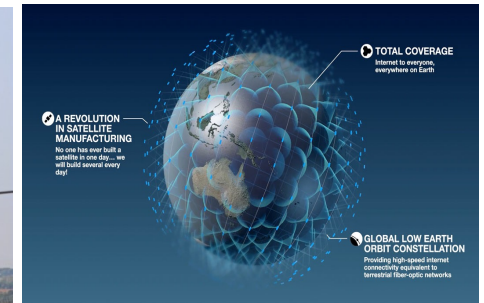


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General Trends around  
classical industrial activities  
=  
**Digitalization**

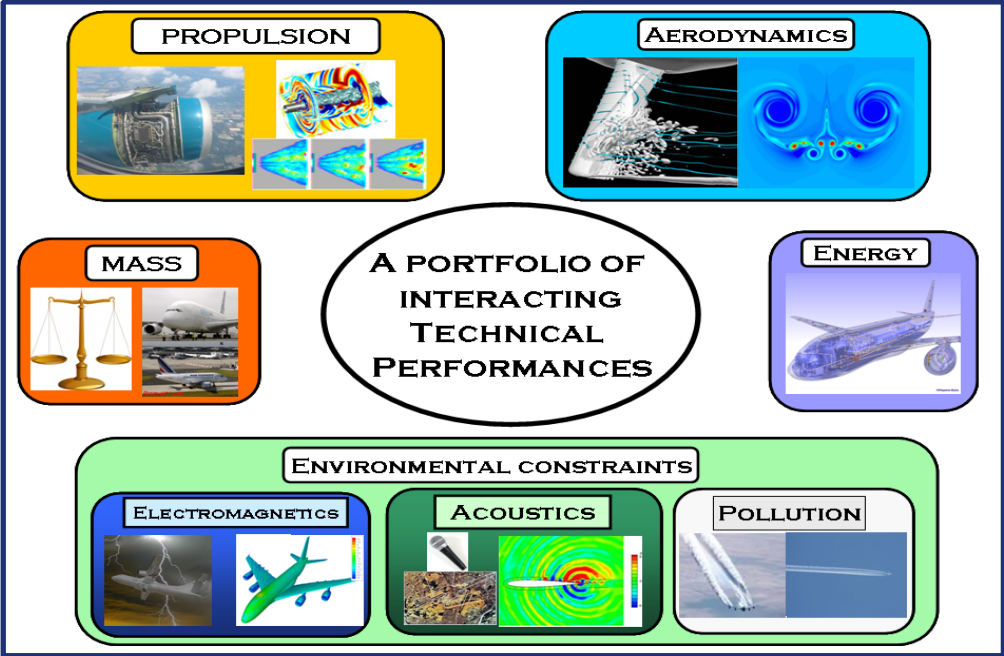
**CURRENT ASSETS & PRODUCT PORTFOLIO**



Flying platforms governed by **complicated** physical laws

« Pure » **physical** behaviors interacting with **Systems & Software**

Delivered through **complex** supply-chain **organisations**



# CURRENT ASSETS & PRODUCT PORTFOLIO



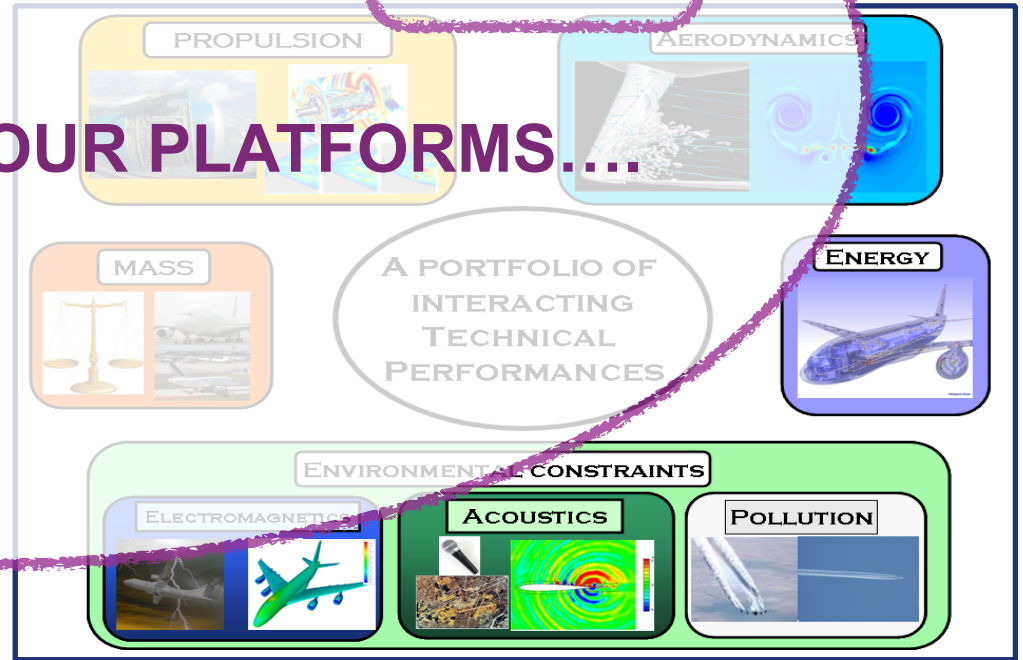
## OUR GOOD UNDERSTANDING OF PHYSICS

## WAS KEY TO BUILD OUR PLATFORMS....

Flying platforms governed by complicated physics laws

« Pure » physical behaviors interacting with Systems & Software

Delivered through complex supply-chain organisations



# EXTERNAL Technological trends in the context of Numerical Optimization

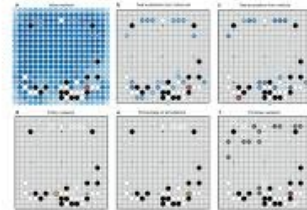
Design & operations are getting closer !



Interactions between vehicles & external systems will increase !



AI algorithms are now available technologies !



AlphaGo

Open Source communities set-up new standards



Design & manufacturing are getting closer (3D ALM) !



Newcomers have adopted more collaborative ways to integrate suppliers !



Computing capabilities are still increasing even if Moore's law is dead!



Big software editors are world players covering 80% of the needs

# EXTERNAL Technological trends in the context of Numerical Optimization

**NEW BUSINESS NEEDS & NEW WAYS OF WORKING ARE EMERGING**

Design & operations are getting closer !

Design & manufacturing are getting closer !

Interactions between vehicles & external systems will increase !

Newcomers have adopted more collaborative ways to integrate suppliers !

**NEW TECHNICAL CAPABILITIES & ACTORS HAVE EMERGED**

AI algorithms are now available technologies !

Computing capabilities are still increasing even if Moore's law is dead!

Open Source communities set-up new standards

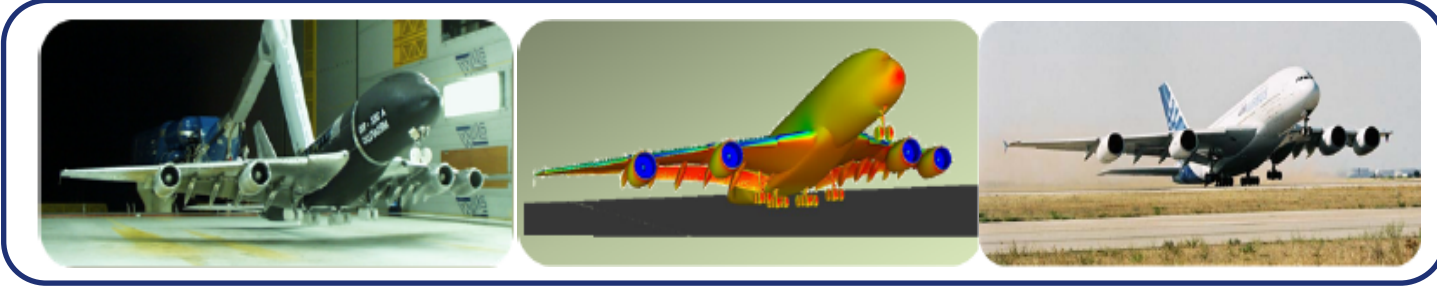
Big software editors are world players covering 80% of the needs



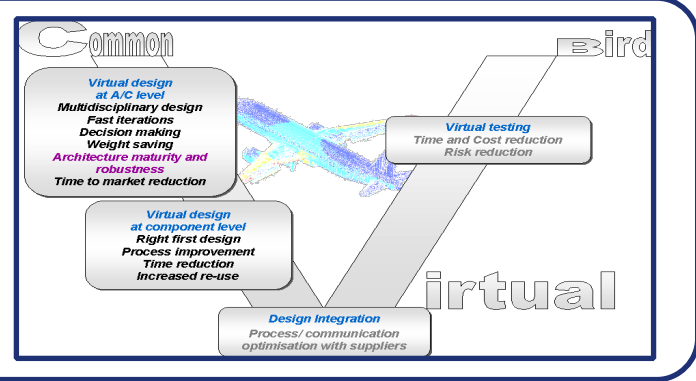
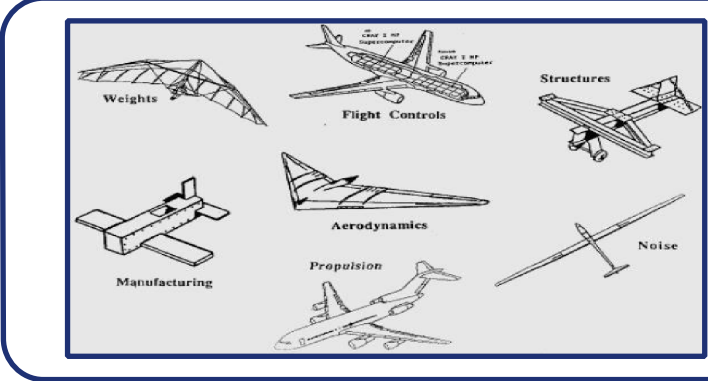
**WHAT IS COMING AROUND ?**

**FACTS**

**FACT** The aerospace engineering knowledge of our physical products is already partly digitalized and detained by Risk Sharing Partners



**FACT** The organisation of simulation is managed in silos mode for different decision gates thus feedback loop is weak between design, testing, manufacturing & operations



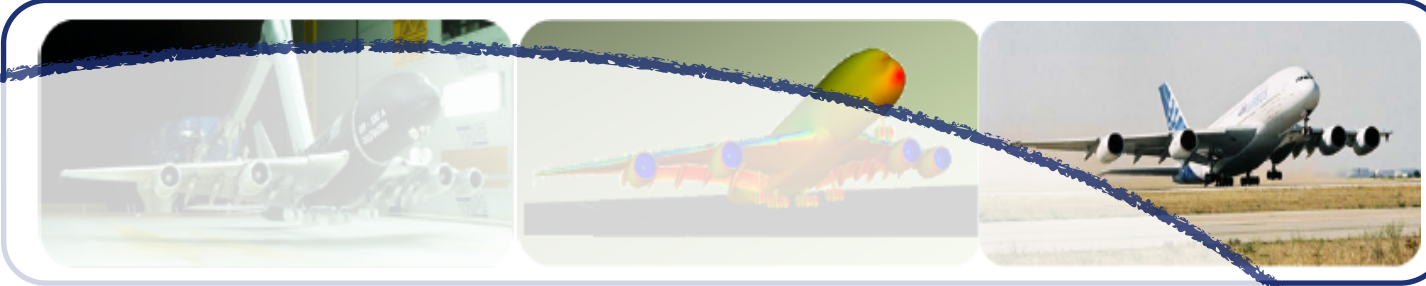
**FACT** New digital systems/apps already collect data/information



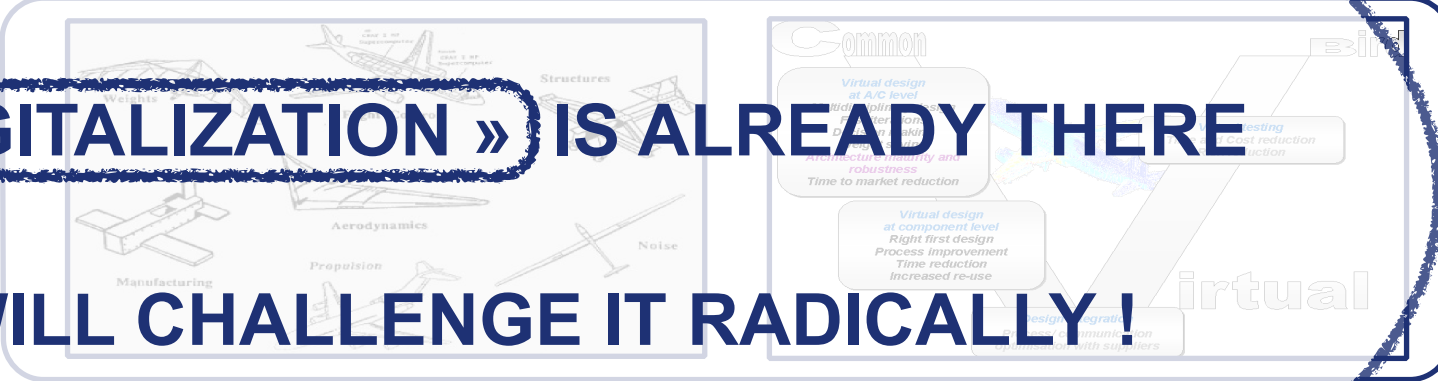
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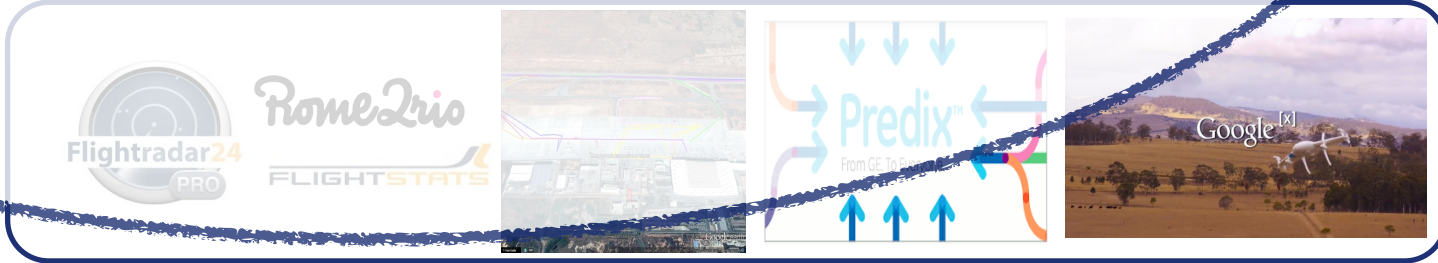
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**FACT** The organisation of simulation is managed in silo mode for different decision gates, thus feedback loop is weak between design, testing, manufacturing & operations



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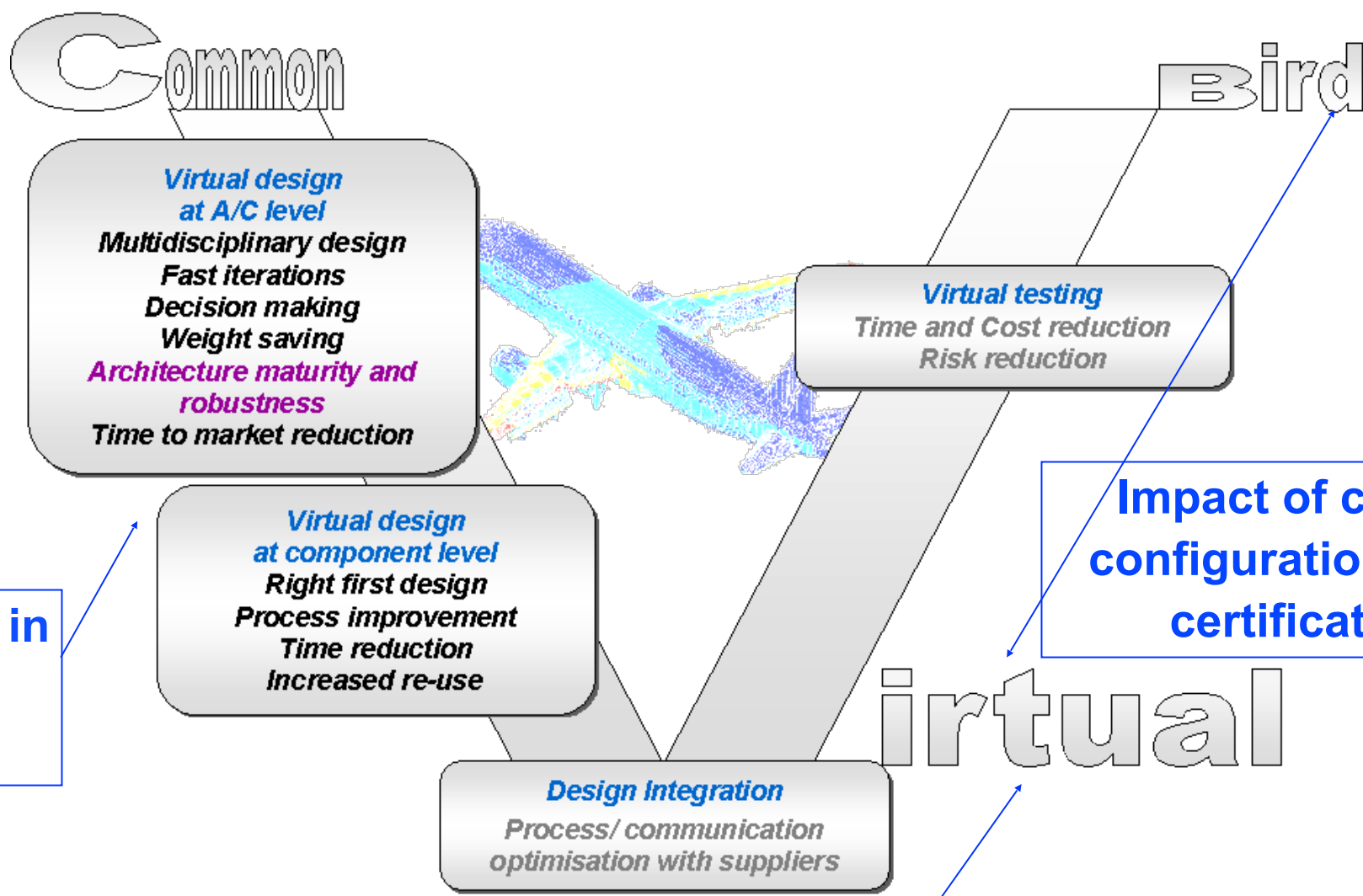


Architects of  
*complex systems*

=

The Challenge in  
**Innovation**

**CLASSICAL objectives associated to Modelling & Simulation processes along the design-cycle**



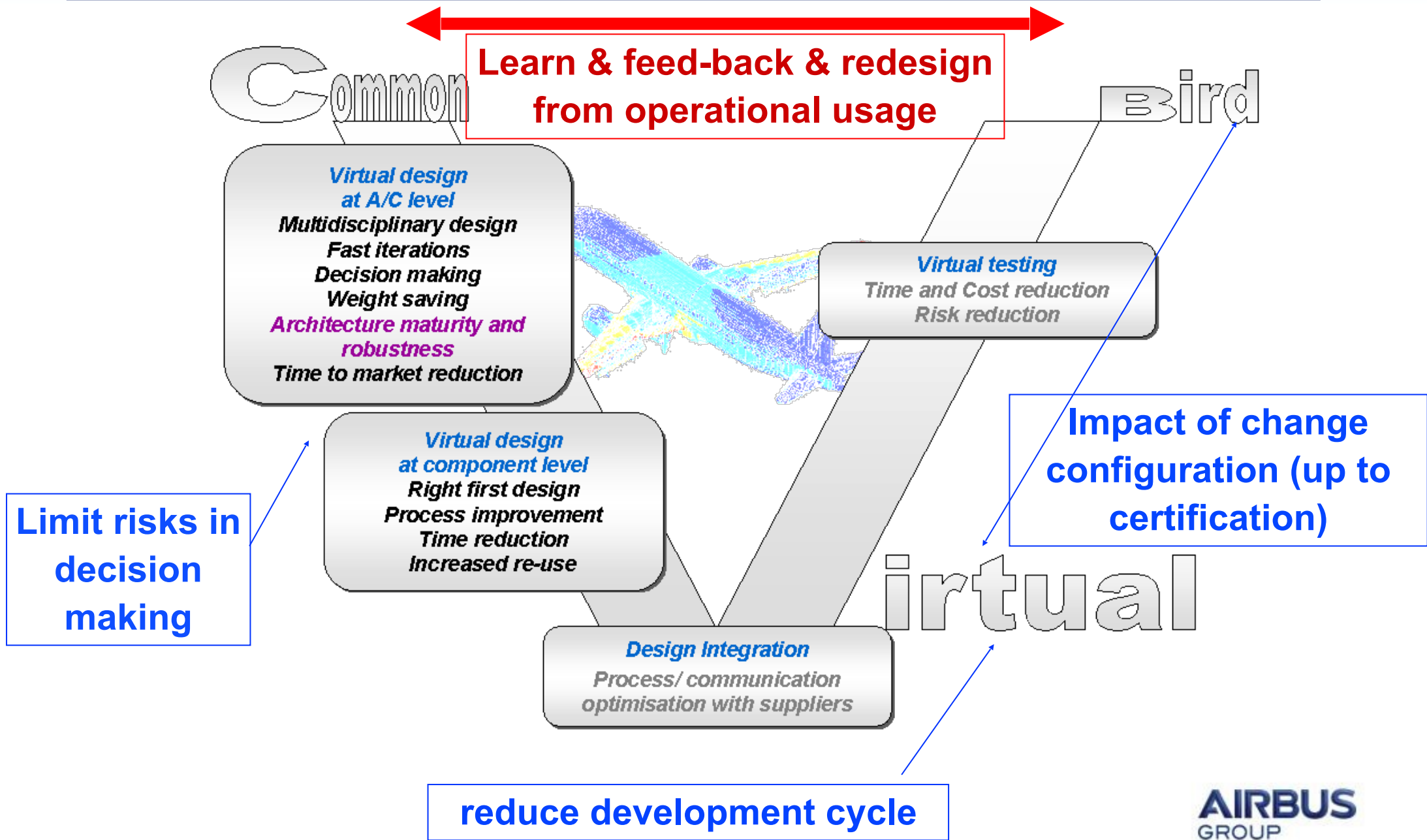
Limit risks in decision making

Impact of change configuration (up to certification)

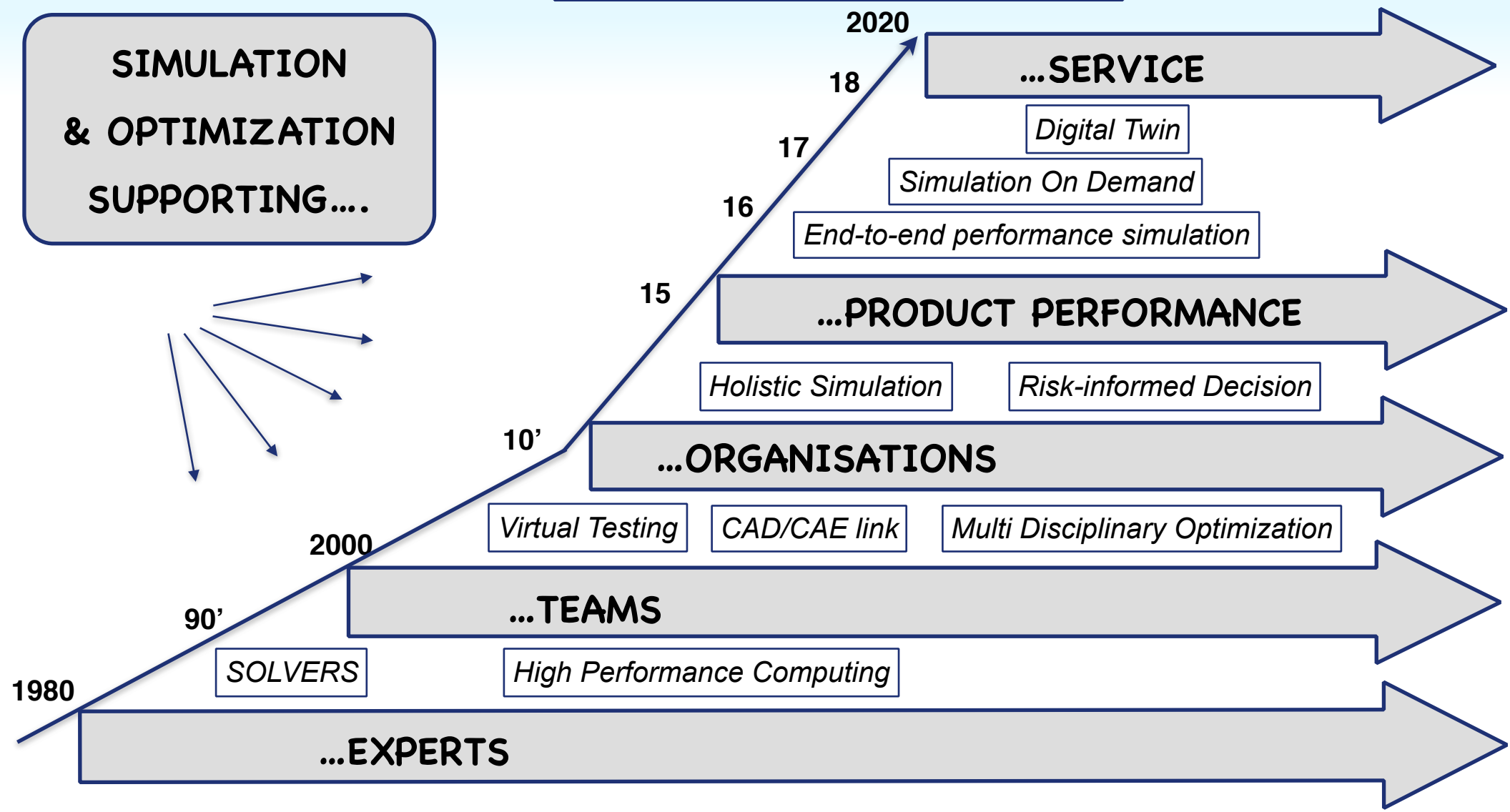
reduce development cycle



**NEW objectives associated to Modelling & Simulation processes along the design-cycle**

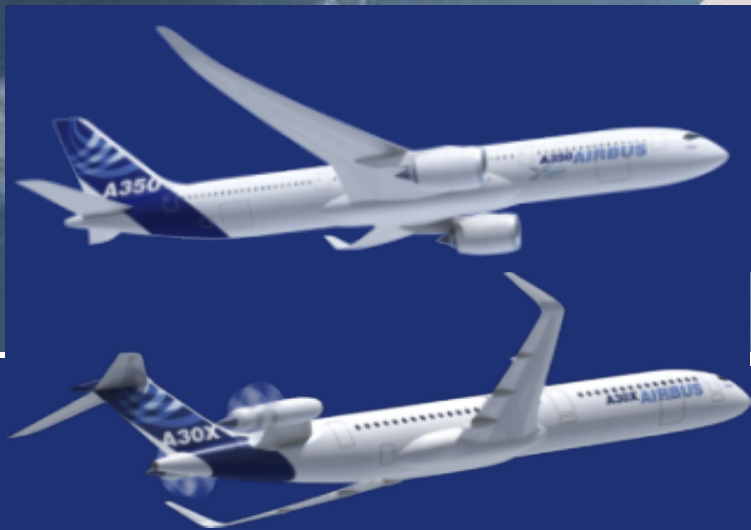


**SIMULATION & OPTIMIZATION SUPPORTING....**



**Simulation&optimisation in industry is not only a matter of developing the right numerical solvers & models !  
It is also related to the stakeholders, their intentions & the organisation around them !**

3



Architect of simulations

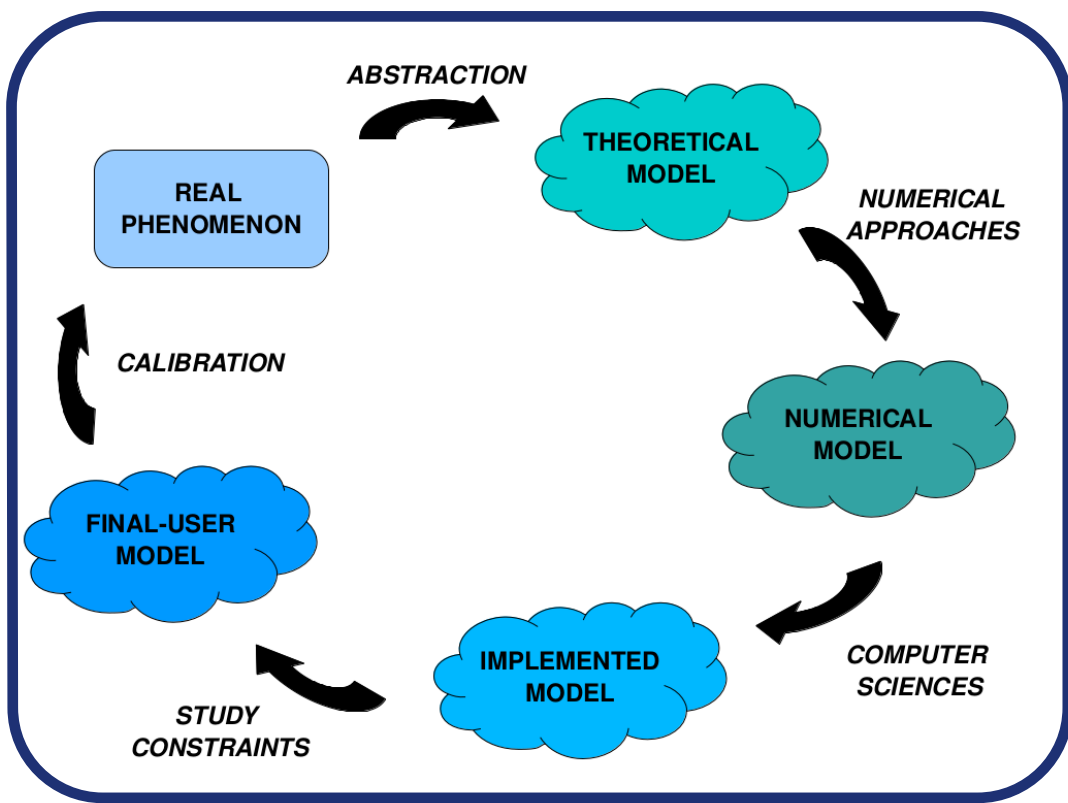
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The Challenges in  
**Optimization**

**MAKE THE DIFFERENCE BETWEEN THE APPLICATIVE WORLD & THE NUMERICAL WORLD**

**APPLICATIVE OBJECTIVES**

- Problem set-up
- Cost
- Physical Constraints
- Optimization
- Value engineering
- Robustness
- Margin
- Performances
- Cost
- Validation
- Systems Engineering



**NUMERICAL WORLD**

- Convergence
- Algorithms
- Mathematical Properties
- Parametrization
- Modelling set-up
- Numerical optimization
- Numerical strategy
- ...

- TOOLS**
- |                        |              |
|------------------------|--------------|
| Information Technology | Software     |
| Deployment             | Scalability  |
| Ergonomy               | Verification |
| Hardware               |              |

**MOVE FROM A PURE MATHEMATICAL MINDSET TO AN ENGINEERING CAPABILITY**





**Challenge 1: MODELLING AN OPTIMIZATION PROBLEM**

**Challenge 2: PARAMETRIZE DESIGN SPACES**

**Challenge 3: MULTI ..... DISCIPLINES / ACTORS / PHYSICS**

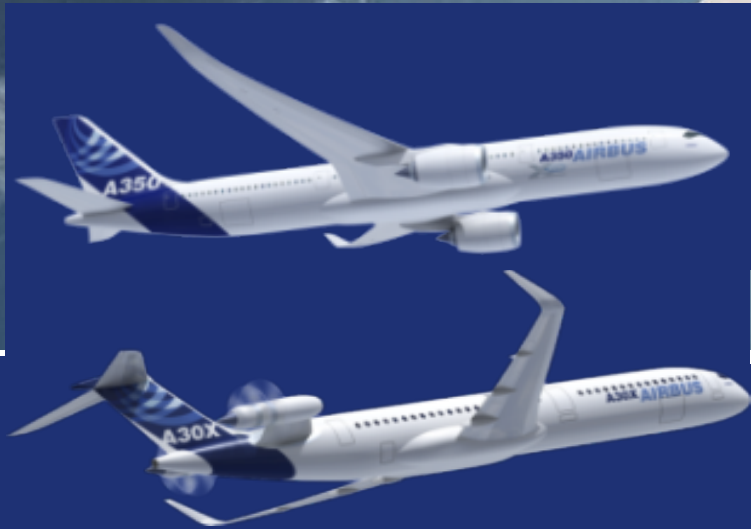
**Challenge 4: IDENTIFY & MEASURE ROBUSTNESS**

**Challenge 5: SCALABILITY & INTERPRETABILITY OF  
ALGORITHMS & RESULTS**

## CHALLENGE 2: PARAMETRIZE DESIGN SPACES

PARAMETRIZATION

3



On-going research activities

**A FEW EXAMPLES TO ILLUSTRATE THE TYPE OF DIFFICULTIES WE ENCOUNTER !**

**GO FROM SPECIFIC CAPABILITIES TO GENERIC CAPABILITIES !**

- **Optimal Positioning of sensors**
- **Topological Optimization in mechanical engineering**
- **Multi Disciplinary Optimization in Aero Elasticity**
- **Uncertainty Management of a Flight Controller**
- **Robust Optimization**

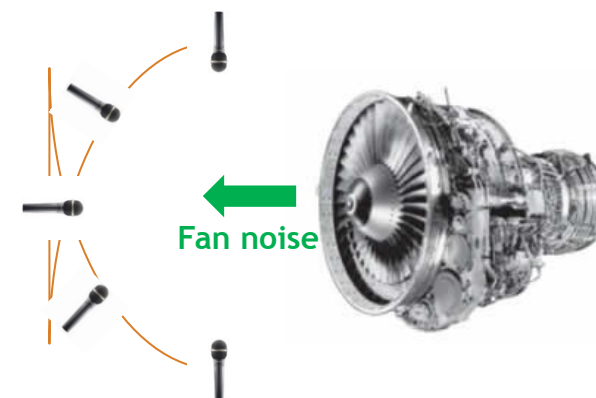
## CHALLENGE 2: PARAMETRIZE DESIGN SPACES

PARAMETRIZATION

# OPTIMAL POSITIONING OF MICROPHONES

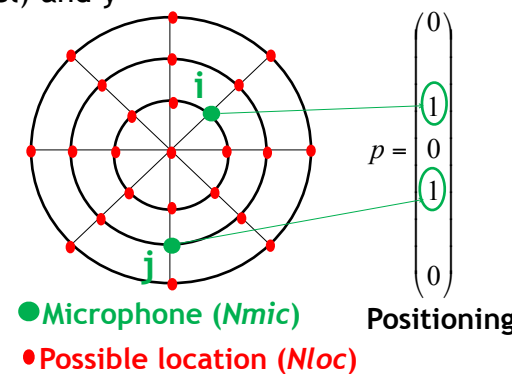
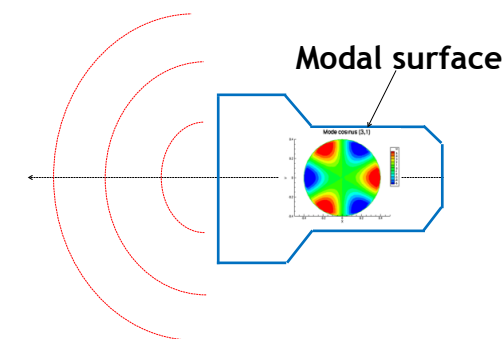
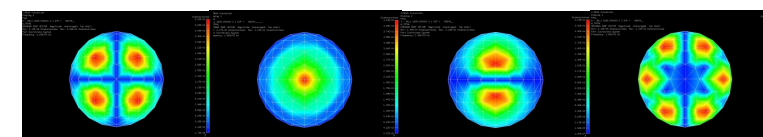
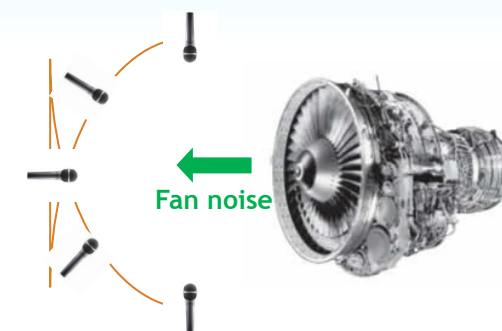
## Objective

- Quieter aircrafts design : need of precise knowledge of noise sources
- Noise is due to interactions between moving parts inside the nacelle
- Once generated, noise propagates inside nacelle and is radiated outside
- Intensive use of numerical modelling
  - **DIRECT model**
  - **INVERSE model** : link with real-life measurements
- Measurement systems using microphones



**OPTIMIZATION PROBLEM**  
 ⇒ Find the most robust microphones  
 positioning  
 that allows to identify at best acoustic sources

# OPTIMAL POSITIONING OF MICROPHONES



Step 0 Direct problem : governing equations

$$\Delta u - \frac{1}{a^2} \frac{\partial^2 u}{\partial t^2} = 0$$

Step 1: Inverse problem

- Problem : given measurement at microphones, find values of modal sources
- Least-squares problem:

$$\alpha^* = \arg \min_{\alpha} \frac{1}{2} \|[T] \cdot \alpha - u\|^2$$

Step 2: Robustness of least-squares problem

• Problem

- For the linear least-squares problem (measurements) are perturbed ?

$$\min_x \|y - Ax\|$$

: how does the solution x changes if A (model) and y

$$p^* = \arg \min_p (\text{cond } T(p))$$

Step 3: Optimal positioning problem - Discrete Formulation

$$p^* = \arg \min_{p \in \text{Sphere}} \text{cond } (T(p))$$

# OPTIMAL POSITIONING OF MICROPHONES

## Direct problem : governing equations

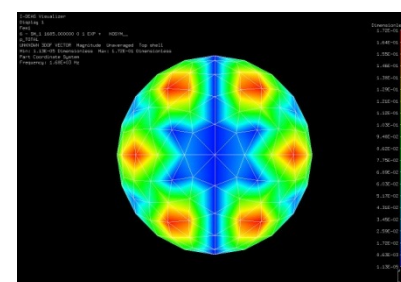
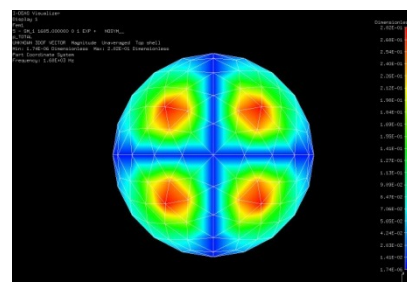
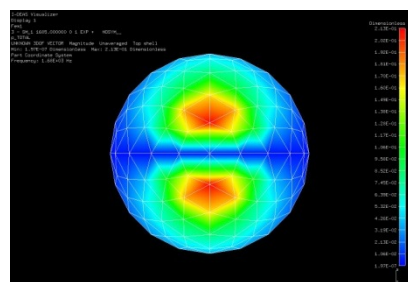
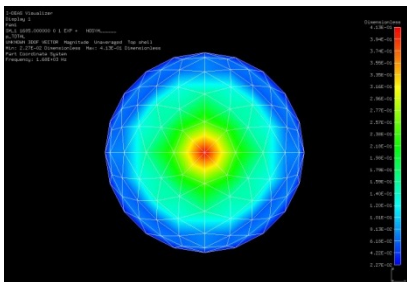
- Sound : waves of pressure propagating through a compressible medium
- Pressure  $u$  is solution of wave equation (time domain)

$$\Delta u - \frac{1}{a^2} \frac{\partial^2 u}{\partial t^2} = 0$$

- HELMHOLTZ equation (frequency domain)

$$\Delta u + k^2 u = 0 \quad \text{with} \quad k = \frac{\omega}{a} = 2\pi \frac{f}{a}$$

- Solution are called the modes  $U_{mn}$  (propagative or evanescent) & **Coefficients of modes  $u_{mn}$  = modal sources**

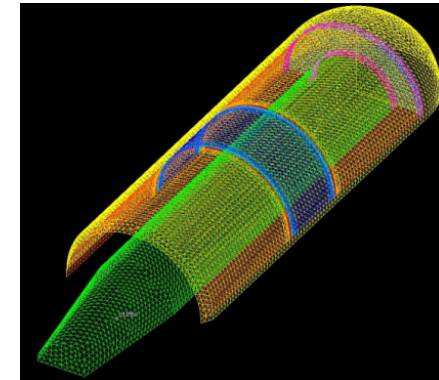




# OPTIMAL POSITIONING OF MICROPHONES

## Direct problem : numerical resolution

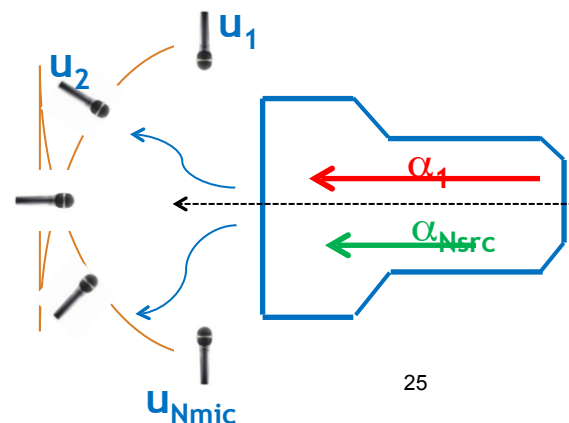
- Numerical resolution of HELMHOLTZ equation :
  - Integral equation formulation
  - Boundary elements method on a triangular mesh
  - Representation theorem
- For a given frequency, pressure at microphones depends linearly on acoustic modal sources



$$\begin{bmatrix} T_{1,1} & \square & T_{1,Nsrc} \\ \square & \square & \square \\ T_{Nmic,1} & \square & T_{Nmic,Nsrc} \end{bmatrix} \cdot \begin{pmatrix} \alpha_1 \\ \square \\ \alpha_{Nsrc} \end{pmatrix} = \begin{pmatrix} u_1 \\ \square \\ u_{Nmic} \end{pmatrix}$$

Nmic : number of microphones  
Nsrc: number of modal sources

### • T : TRANSFER MATRIX



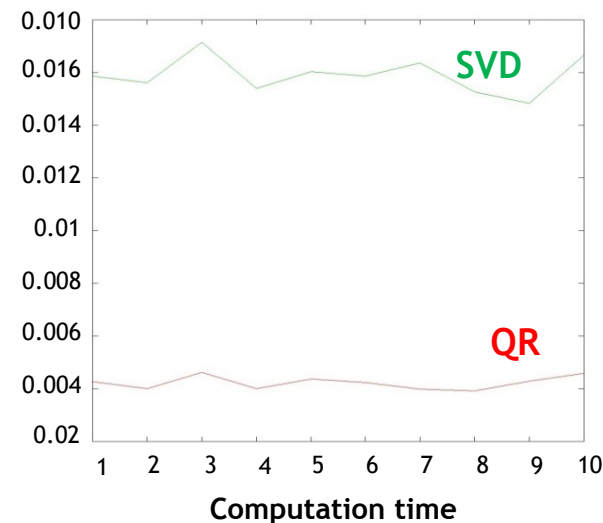
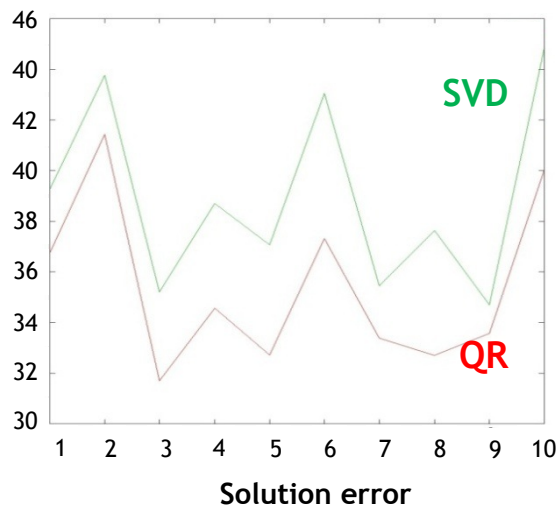
# OPTIMAL POSITIONING OF MICROPHONES

## Step 1: Inverse problem

- Problem : given measurement at microphones, find values of modal sources
- Least-squares problem:
- Until recently, resolution based on SVD

$$\alpha^* = \arg \min_{\alpha} \frac{1}{2} \|[T] \cdot \alpha - u\|^2$$

- Comparisons SVD - QR on typical samples



⇒ QR more suitable for solving inverse problem

⇒ Nevertheless, SVD useful for computing condition number

⇒ What is the robustness of the solution  $\alpha$  with respect to error on microphones positioning ?

# OPTIMAL POSITIONING OF MICROPHONES

## Step 2: Robustness of least-squares problem

### • Problem

- For the linear least-squares problem  $\min_x \|y - Ax\|$  : how does the solution  $x$  changes if  $A$  (model) and  $y$  (measurements) are perturbed ?

### • Sensitivity analysis

- Note  $\Delta x$  the perturbation on sources due to a perturbation  $\Delta y$  (resp.  $\Delta A$ ) on measurements (resp. model)

$$\frac{\|\Delta x\|}{\|x\|} \leq \text{cond}(R) \frac{\text{lub}(\Delta A)}{\text{lub}(A)} + \text{cond}(R)^2 \frac{\|r\|}{\text{lub}(A)\|x\|} \frac{\text{lub}(\Delta A)}{\text{lub}(A)} + \text{cond}(R) \frac{\|y\|}{\text{lub}(A)\|x\|} \frac{\|\Delta y\|}{\|y\|}$$

### • Interpretation

- $\frac{\|\Delta x\|}{\|x\|}, \frac{\|\Delta y\|}{\|y\|}, \frac{\text{lub}(\Delta A)}{\text{lub}(A)}$  : relative errors on source, measurements & model
- Error on source identification proportional to matrix  $R$  conditioning (from QR decomposition of  $A$ )

### • Conclusion :

Robust positioning  $p$  in regard to sources accuracy

=

**Find the positioning that minimizes the condition number of  $R$  (and consequently  $T$ ) !**

$$p^* = \arg \min_p (\text{cond } T(p))$$

# OPTIMAL POSITIONING OF MICROPHONES

## Step 2: Optimal positioning problem

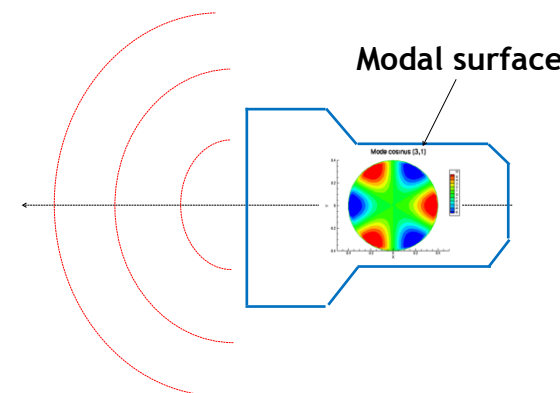
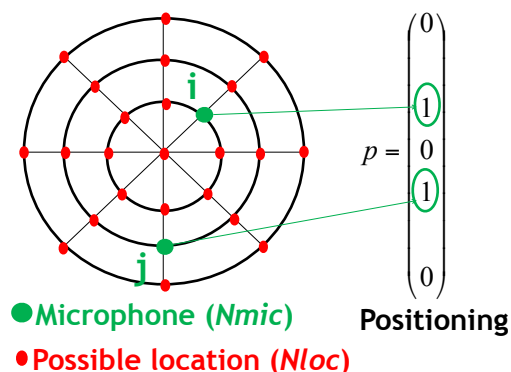
- Optimal positioning problem

$$p^* = \arg \min_p (\text{cond } T(p))$$

- Classical gradient-based method not adapted for such a cost function
- Global Optimization problem with many local minima
- Discretization of search space to switch to a combinatorial problem
- Link to methods of Operational Research
- Original approach in Acoustics

# OPTIMAL POSITIONING OF MICROPHONES

- Noise propagation assumed to be isotropic outside the engine
- Radiation on a semi-sphere contains information of a same modal surface
- Hence, microphones are searched on a discretized semi sphere of Nloc possible positions



## Step 3: Optimal positioning problem - Discrete Formulation

$$p^* = \arg \min_{p \in Sphere} \text{cond}(T(p))$$

- Transfer matrix

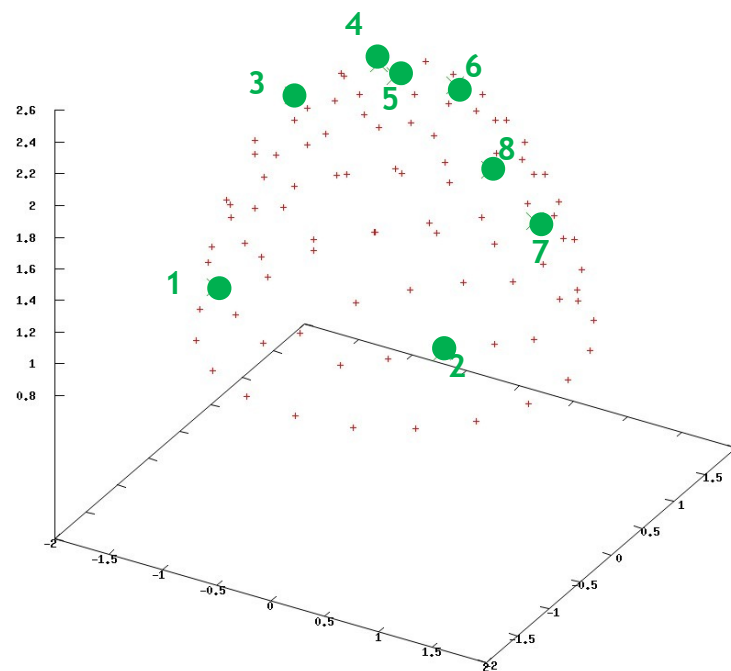
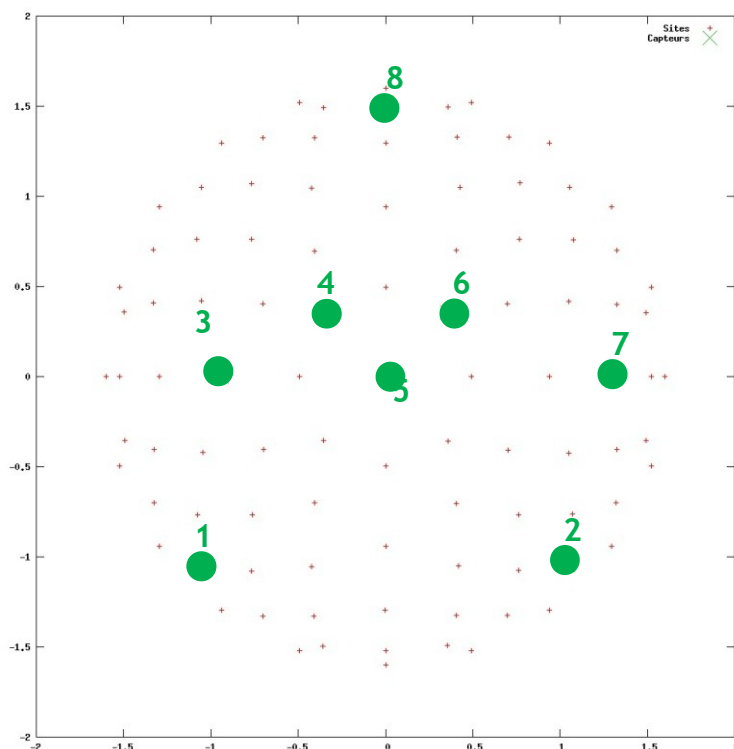
Global transfer matrix :  $[ T^{GLOB} ]$   
 &  
 Transfer matrix restriction  
 to microphones subspace :  $[ T(p) ]$

$T_{1,1}$	$T_{1,2}$	...	$T_{1,Nsrce}$
$T_{2,1}$	$T_{2,2}$	...	$T_{2,Nsrce}$
...	...	...	...
$T_{i,1}$	$T_{i,2}$	...	$T_{i,Nsrce}$
$T_{j,1}$	$T_{j,2}$	...	$T_{j,Nsrce}$
...	...	...	...
$T_{Nloc,1}$	$T_{Nloc,2}$	...	$T_{Nloc,Nsrce}$

# OPTIMAL POSITIONING OF MICROPHONES

Case with a good condition number  
 Reconstruction of 8 modal sources with 8 microphones  
 Semi sphere discretization : 100 points

Sites  
 Capteurs



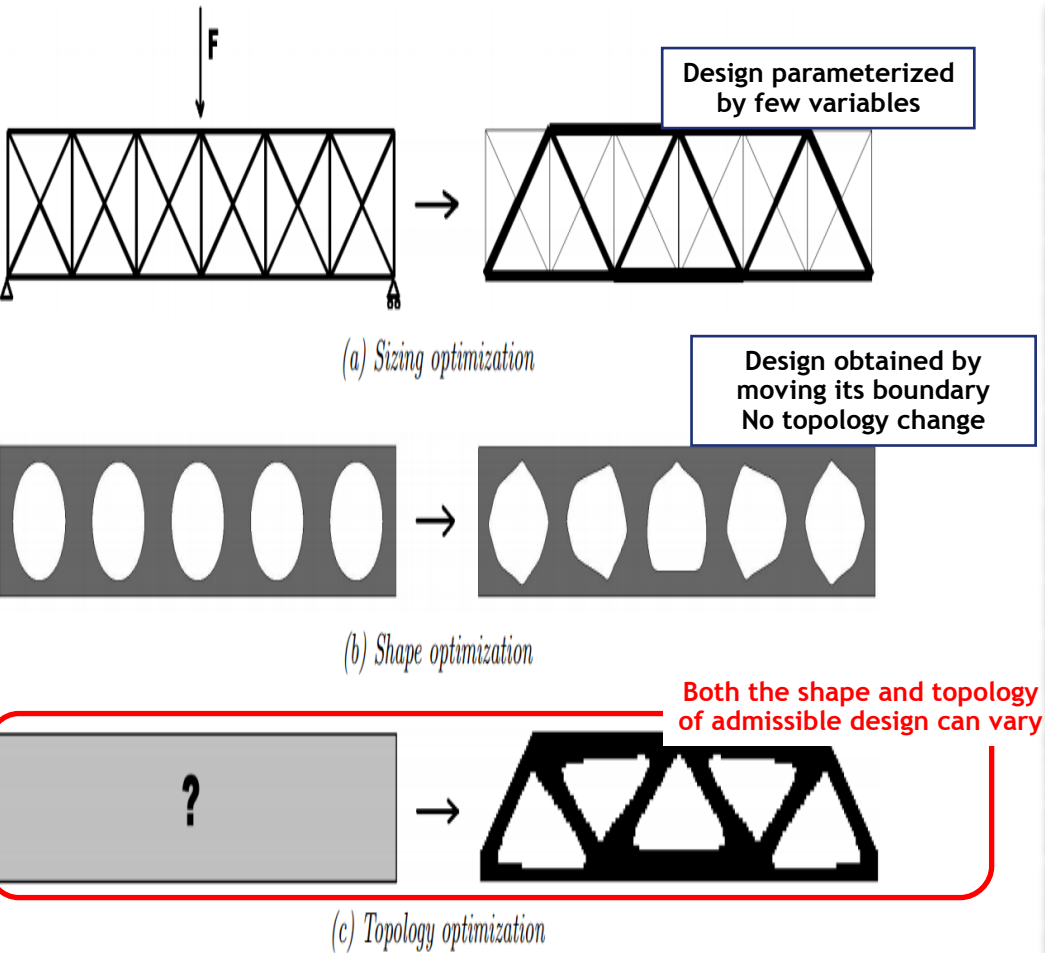
Optimal positioning: far from practitioner experience !

# OPTIMAL POSITIONING OF MICROPHONES

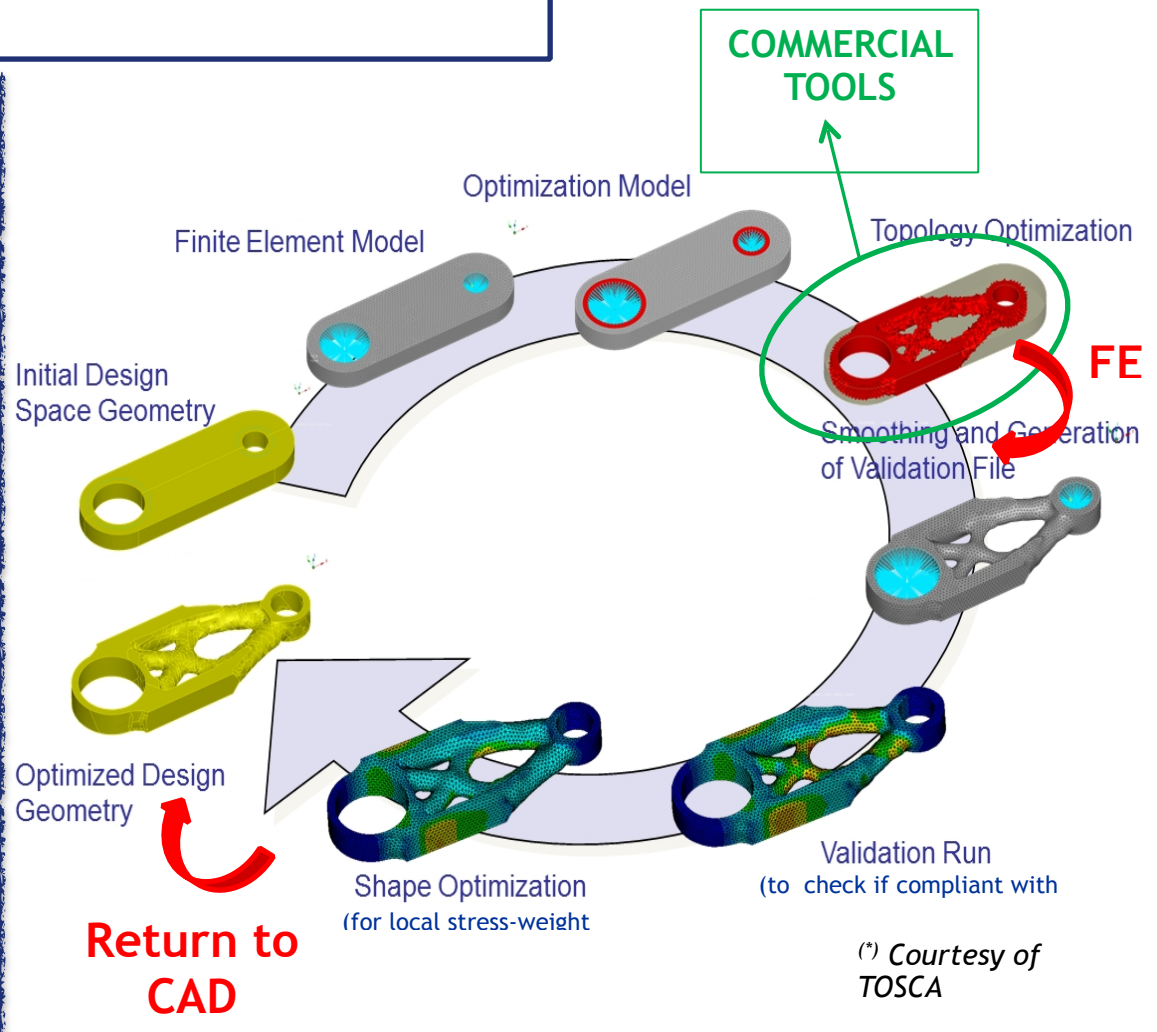
## Next steps

- Validate/Enrich the Optimization Positioning capabilities for test engineering
  - Validation, tests & benchmarks
  - Integrate test set-up constraints
- Generalize this approach to other physics
  - Electromagnetism
  - Vibro acoustics,
  - Thermics
  - Aerodynamic
- System View: Make the link with test engineering practices

# TOPOLOGICAL OPTIMIZATION



Typology of optimization problems



**Goal: From numerical optimization to engineering capability**

(\*) Courtesy of TOSCA



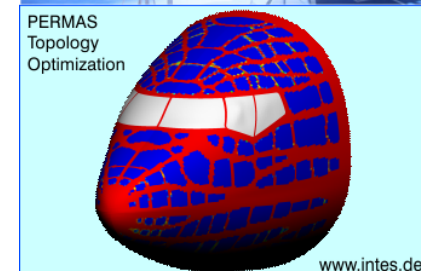
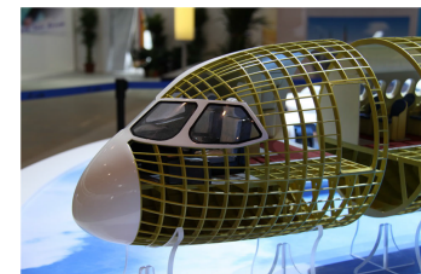


# TOPOLOGICAL OPTIMIZATION

- Why industrials could be interested in Topology Optimization (TO)
  - Ease of use : “just” to provide specifications & design space in geometrical terms
  - Gain in mass : between 3% & 15% obtained on “simple” structures
  - Find new “breakthrough” configurations



- Therefore, TO is not used systematically & field of applications remains modest
- Mainly due to the fact that today methods & tools :
  - Generate only a concept, far from being manufactured
  - Limited to simple structures, physical analysis & constraints
  - Not easily pluggable into the design process (remeshing, no return ...)



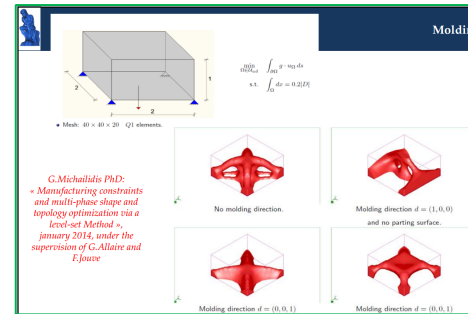
# TOPOLOGICAL OPTIMIZATION

Results of the **RODIN project** (FUI project supported, System@tic)  
 Industrial Partners: Renault, Airbus Group, Safran Tech, ESI, DPS, EuroDecision  
 Academic Partners: Ecole Polytechnique CMAP, University Paris VI Lab JLL, INRIA



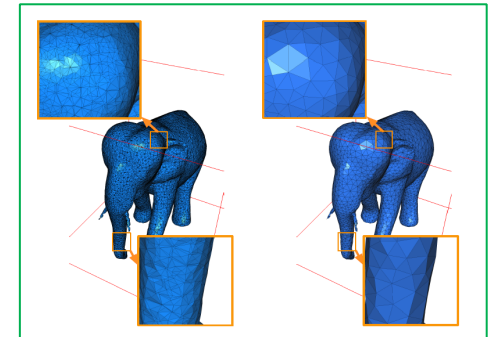
- Numerical ingredients:
- Level-set method
  - Shape sensitivity analysis
  - Topological derivative
  - FEM mesh & cartesian grid - Local remeshing

## Molding



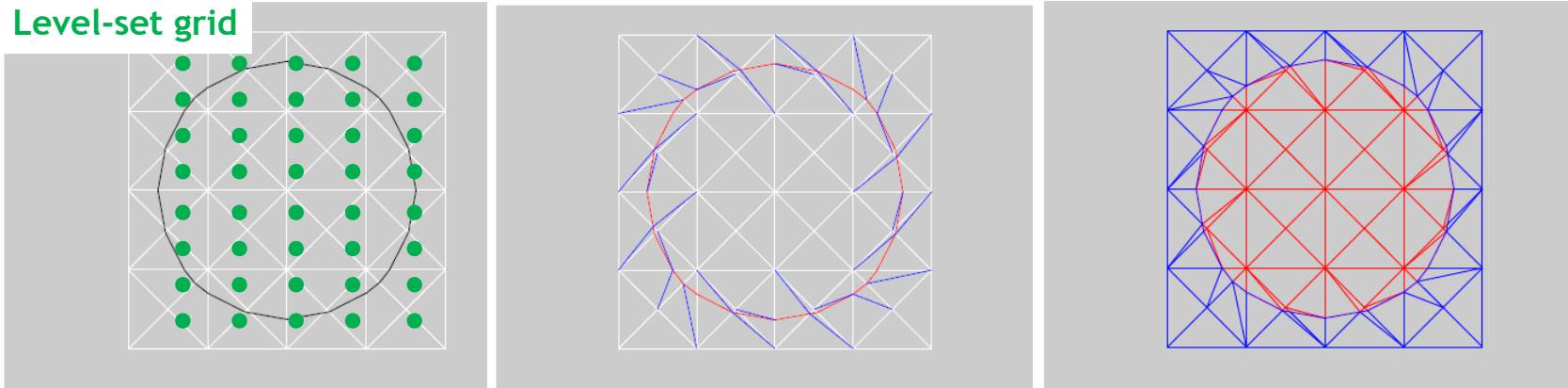
PhD G. Michailidis

## Local remeshing



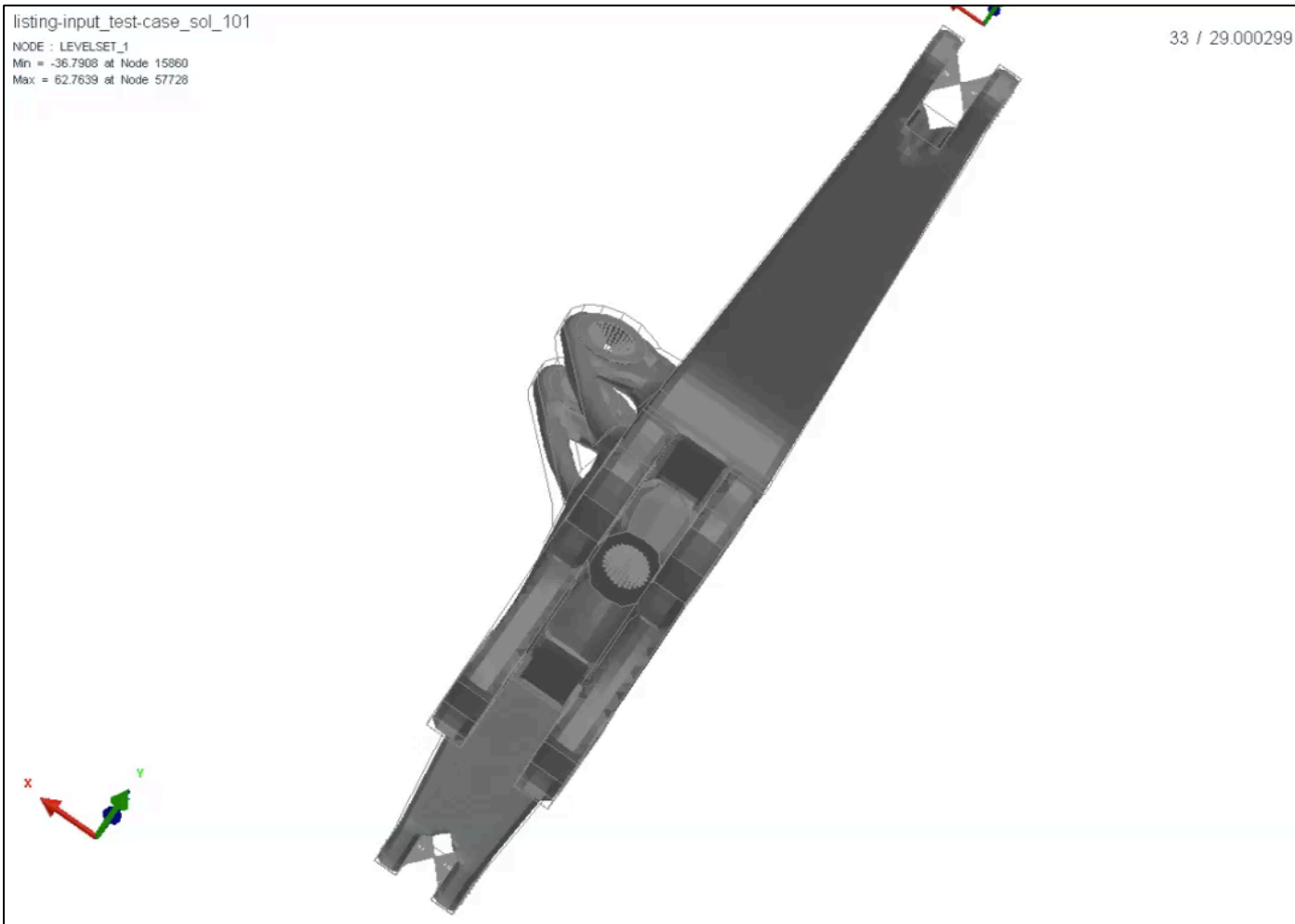
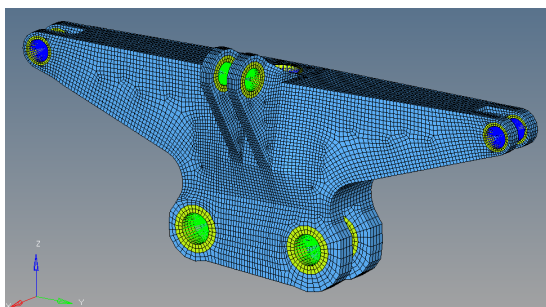
PhD Ch. Dapogny

## Level-set grid

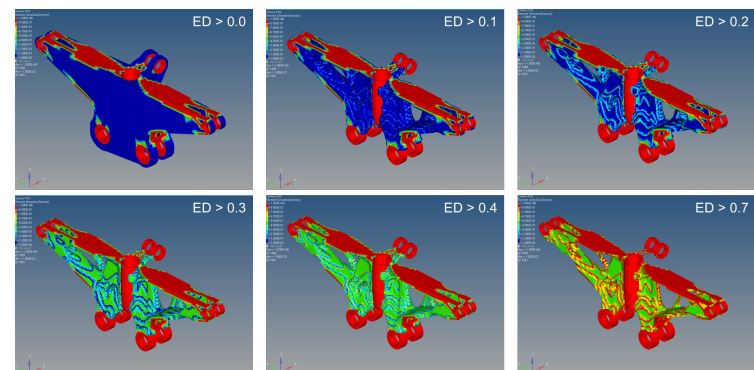


# TOPOLOGICAL OPTIMIZATION

## Engine bracket test-case



- Based on NASTRAN model: All Solid elements retained
- Displacement constraint set to 6 mm
- 14 Loads used from NASTRAN model
- Mass minimization s.t. displacement constraints



Results obtained within RODIN project

Results based on SIMP method

# TOPOLOGICAL OPTIMIZATION

## Next steps

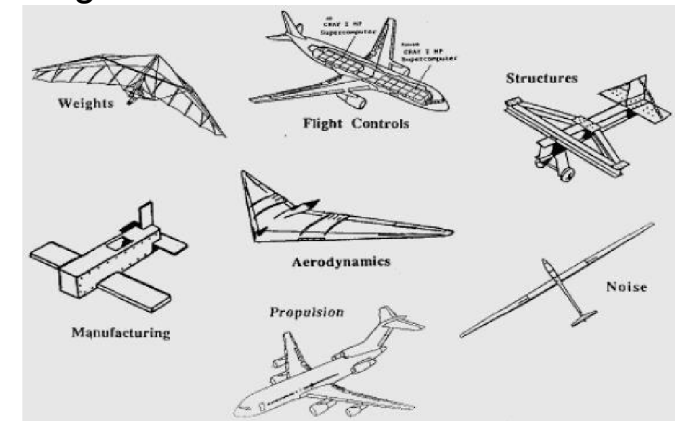
- Validate/Enrich the Topological Optimization capabilities for mechanical engineering
  - Validation, tests & benchmarks
  - Extension of physical analysis (contact, thermo-elasticity,...)
  - Multi-phases structures & non-linear materials
  - Introduction of ALM constraints both from geometrical or simulation viewpoint
- Generalize the Topological Optimization capabilities for other physics
  - Vibro acoustics,
  - Thermics
  - Aerodynamic
- System view: Make the link with detailed design engineering & classical work breakdown structures organisations

# MULTI DISCIPLINARY OPTIMIZATION

- **Challenge in aircraft design**

- Design “next generation” aircrafts, with conceptual & technological breakthrough
- Many disciplines are concerned
- But, today disciplines are generally handled separately and sequentially

**Sequential design = risk of local solutions & antagonistic decisions**



- **Goal of MDA/MDO**

- Handle the disciplines simultaneously and exploit efficiently their interactions

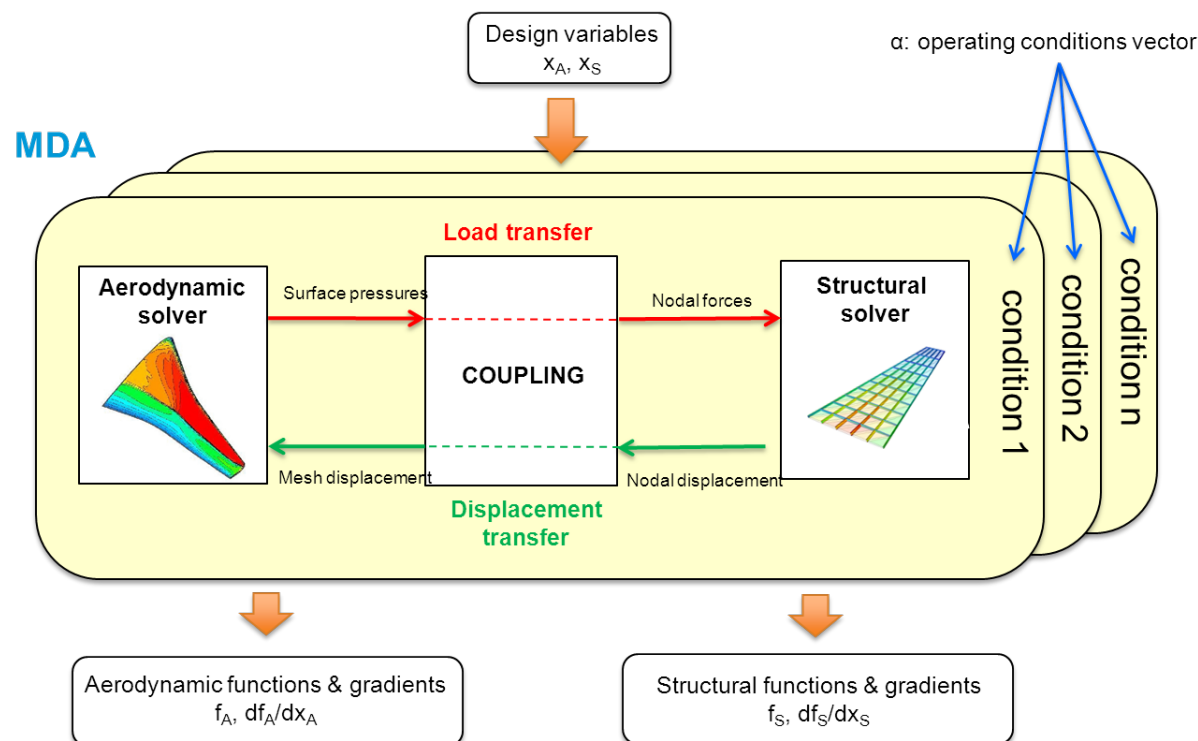
**Simultaneous design = better optimum & trade-off analysis**

- **Our current challenge is focused on wing aero-structure coupling but the mathematical formulation is general and can be extended to any number of disciplines**

# MULTI DISCIPLINARY OPTIMIZATION

## MDA : Multidisciplinary Design Analysis

- Shape is fixed
- Aims at finding the physical equilibrium between disciplines



### 2 important topics

#### 1. Operating conditions

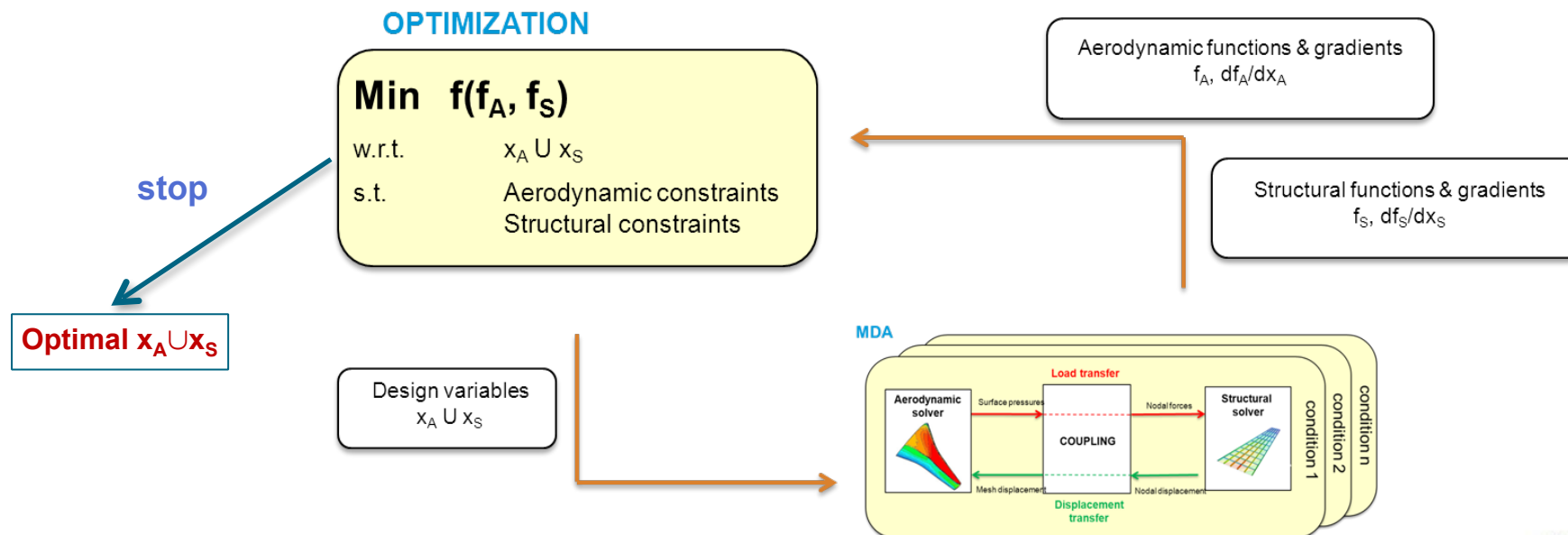
A very important concept that determines the choice of disciplinary fidelity level

#### 2. Coupling

Methods for solving efficiently the MDA problems

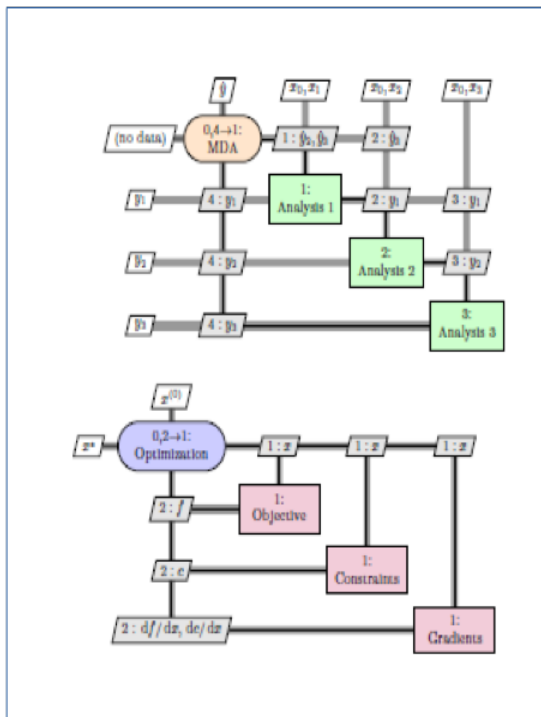
# MULTI DISCIPLINARY OPTIMIZATION

- Search to find the best shape that minimizes one or several criteria
- Could just consist in plugging an optimization algorithm to MDA process
- But many others strategy could be implemented (IDF, BLISS,..) ⇒ **this is the goal of MDO as research field**

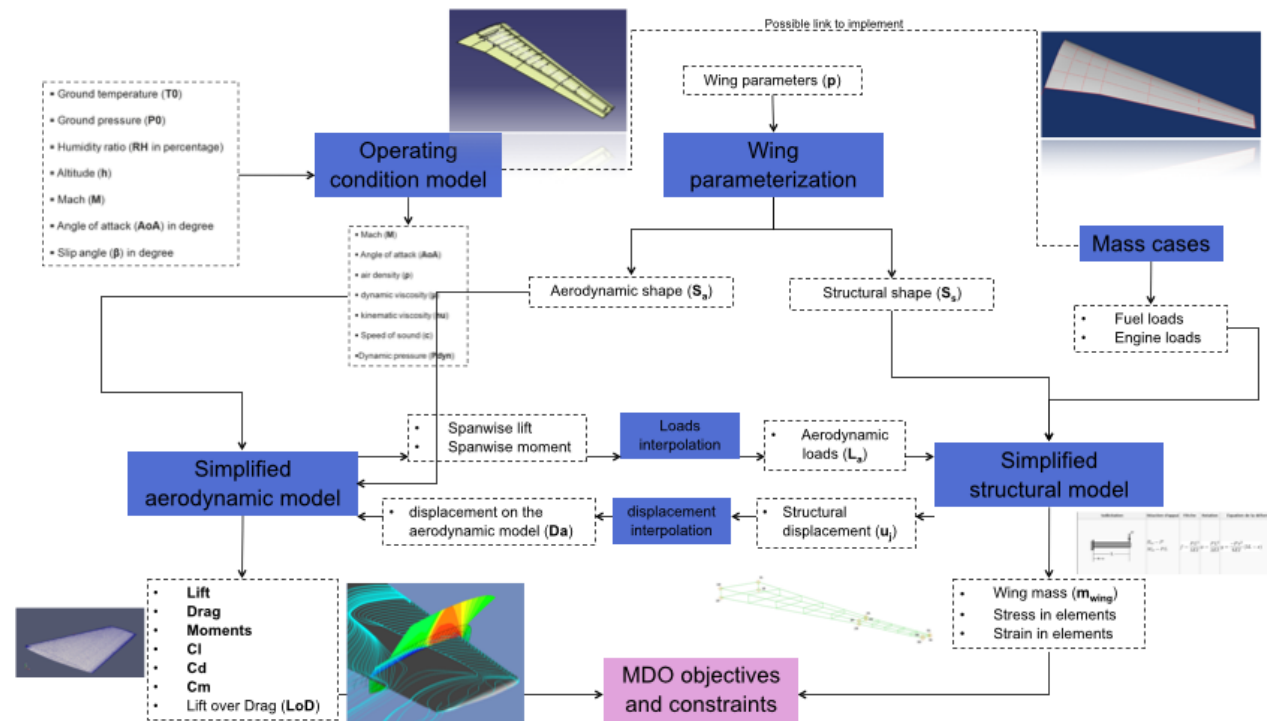


# MULTI DISCIPLINARY OPTIMIZATION

## MDO data exchange



Generic representation of a numerical MDO process



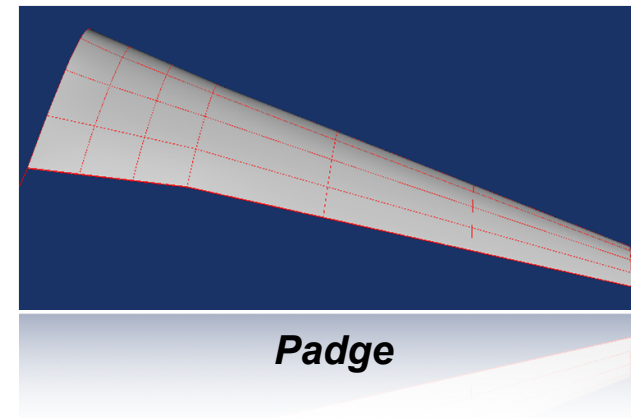
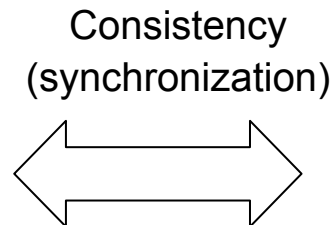
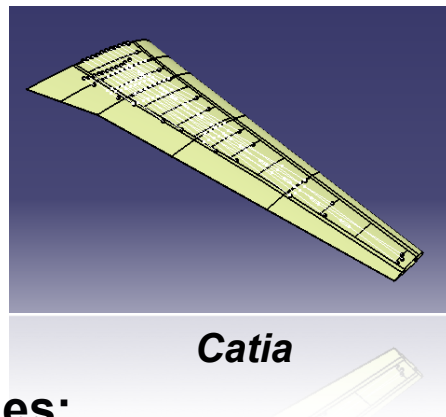
Use-case associated to the aero elastic context



# MULTI DISCIPLINARY OPTIMIZATION

## Purpose of Multi-disciplinary parameterization

The purpose of the multidisciplinary parameterization is to ensure the **models consistency** required by MDO activities. The different models (struct, Aero, ...) has to **be consistent according to their sets of parameters** and the set of parameter is considered as the **only way to monitor geometry update/transformation !**



### Challenges:

- Impact changes of **structure model to aerodynamic model**
- Impact changes of **aerodynamic model to structure model**
- Ensure models integration between two **different geometric kernels**
- **Automatize model interaction** for optimization loops

# MULTI DISCIPLINARY OPTIMIZATION

## Next steps

- Understand the Multi Optimization capabilities for aero elastic problems
  - Validation, tests & benchmarks
  - Extension of physical analysis (low/high fidelity → adequacy)
- Generalize the Multi Optimization capabilities for other physics
  - Acoustics,
  - Thermics
  - System models (0D-1D)
- System view: Make the link with detailed design engineering & classical work breakdown structures organisations

# UNCERTAINTY MANAGEMENT

## System of interest

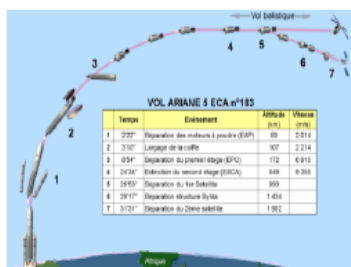


Figure: Mission description



Figure: Atmospheric flight

- A controller (*ie* a numerical strategy) **C** is defined over a set of input variables  $(x, \theta)$  to perform a virtual test corresponding to the flight time interval  $[0, T]$ .
- The behaviour of the system is observed through the state variables  $s$  (*deflection, consumption, attitude, ...*).
- The performances of the controller **C** are qualified through the belonging of the output variables  $y = (\kappa \circ C)(x, \theta)$  to a given numerical domain  $\mathcal{D}$  (*exceedance or not of a threshold, ...*).

## Uncertainty arising in the applicative context

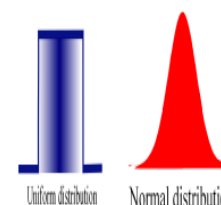


Figure: Uncertainties

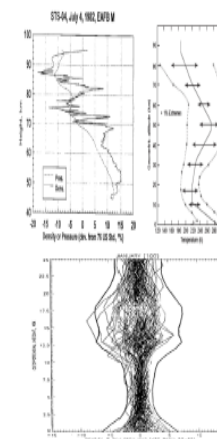


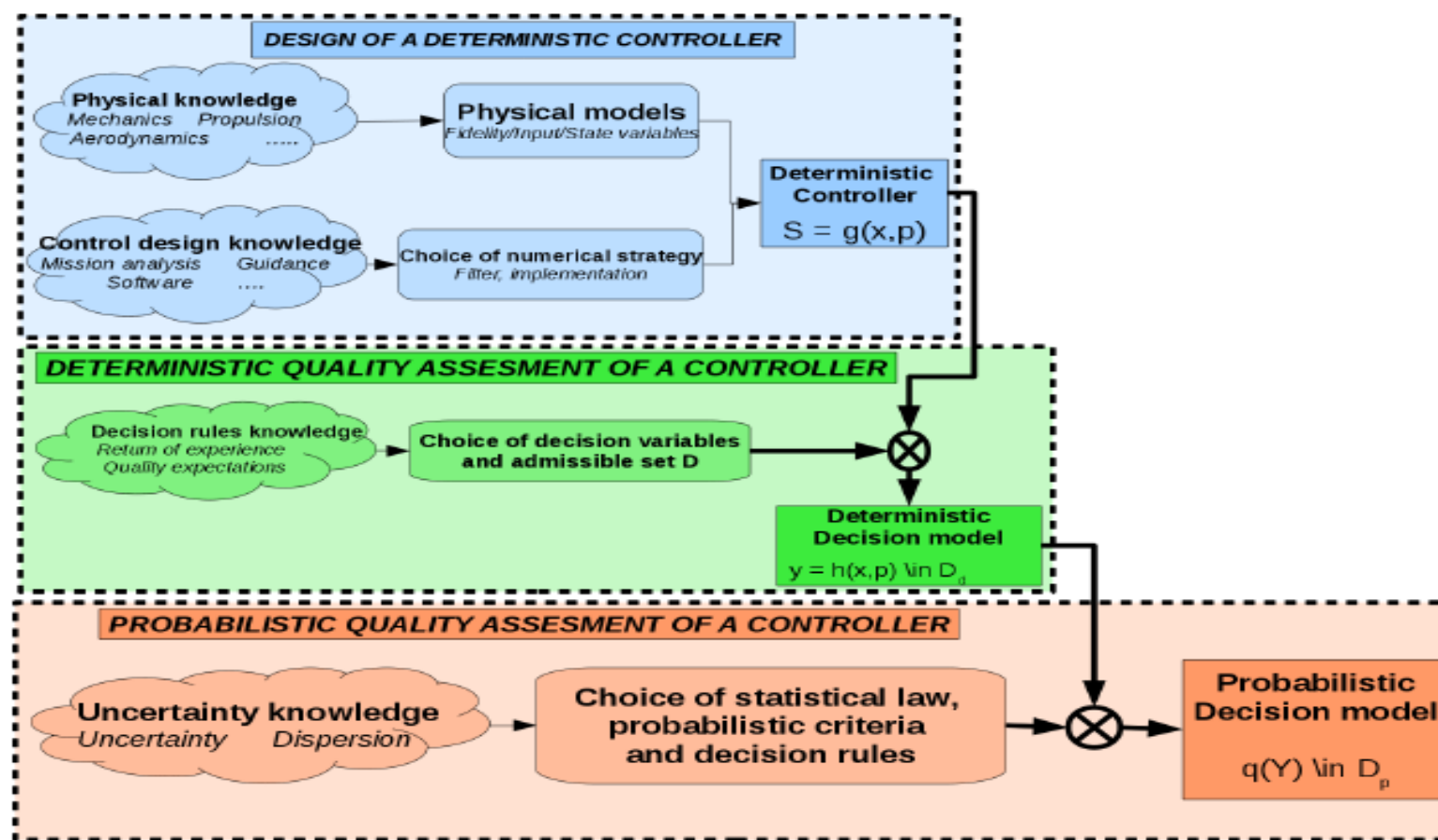
Figure: Wind model

Uncertainties and dispersions in this context

- **Uncertainties** correspond to the lack of knowledge of the values taken by some input variables (*rigid dynamic, bending modes*). This uncertainty could be reduced in some cases by an increase of knowledge (better model, return of experience) or NOT (unknown unknown!).
- **Dispersions** correspond to observed variability, most often small variability around a nominal value.

# UNCERTAINTY MANAGEMENT

## Synoptic of the technical activities



# UNCERTAINTY MANAGEMENT

## Application to the design of a deterministic controller

- **Input variables**  $x \in \mathbb{R}^P$  ( $P = 35$ ):  
 $x = (\text{Rigid Dynamic, Bending Modes, Wind Model})$
- **State/output variables**  $y \in \mathbb{R}^Q$  ( $Q = 6$ ):  
 $y = (\text{Deflection } (d(t)), \text{ Consumption } (c(T)), \text{ Dynamical Load } (q_\alpha(t)), \text{ Attitude During Flight } (\alpha(t)), \text{ Final Attitude } (\alpha(T)), \text{ Final Angular Rate } (\dot{\alpha}))$
- **Controller:**  $h : x \in \mathbb{R}^{35} \rightarrow y \in \mathbb{R}^6$  considered like a black-box

### Deterministic requirements

$$\left\{ \begin{array}{l} \text{D: } y_1 \leq d_0 \\ \text{C: } y_2 \leq c_T \\ \text{DL: } y_3 \leq q_\alpha^0 \\ \text{ADF: } y_4 \leq a_0 \\ \text{FA: } \|y_5\| \leq k * \alpha_T \\ \text{FAR: } y_6 \leq \alpha_0 \end{array} \right.$$

### Probabilistic requirements

$$\left\{ \begin{array}{l} \text{D: } \mathbb{P}(\{\omega \in \Omega : y_1(\omega) \leq d_0\}) \leq \beta_1 \\ \text{C: } \mathbb{P}(\{\omega \in \Omega : y_2(\omega) \leq c_T\}) \leq \beta_2 \\ \text{DL: } \mathbb{P}(\{\omega \in \Omega : y_3(\omega) \leq \bar{q}_\alpha\}) \leq \beta_3 \\ \text{ADF: } \mathbb{P}(\{\omega \in \Omega : y_4(\omega) \leq a_0\}) \leq \beta_4 \\ \text{FA: } \mathbb{P}(\{\omega \in \Omega : y_5(\omega) \leq k * \alpha_T\}) \leq \beta_5 \\ \text{FAR: } \mathbb{P}(\{\omega \in \Omega : y_6(\omega) \leq \alpha_0\}) \leq \beta_6 \end{array} \right.$$

# UNCERTAINTY MANAGEMENT

## Propagation of uncertainty

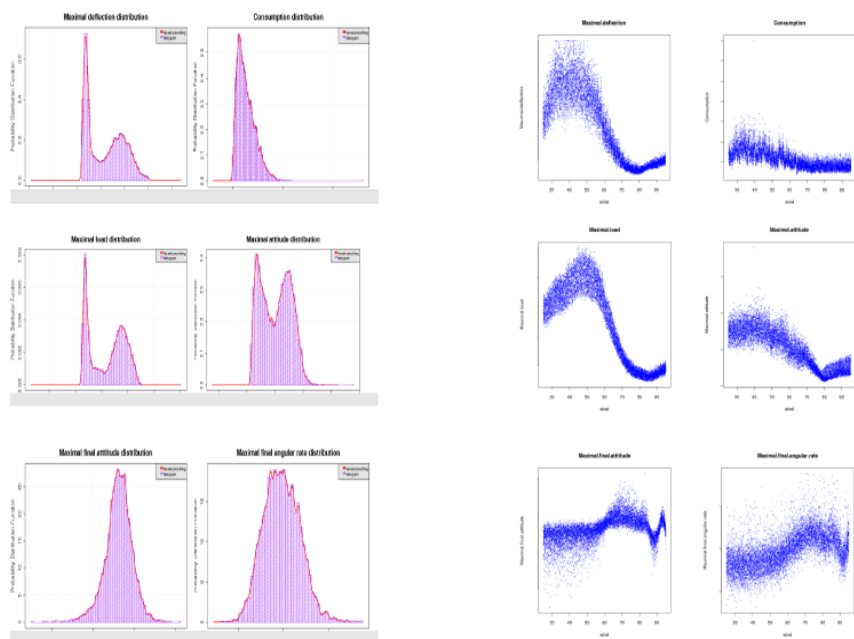


Figure: Uncertainties on outputs

Figure: Outputs vs wind model inputs

## Sensitivity indexes of a probability

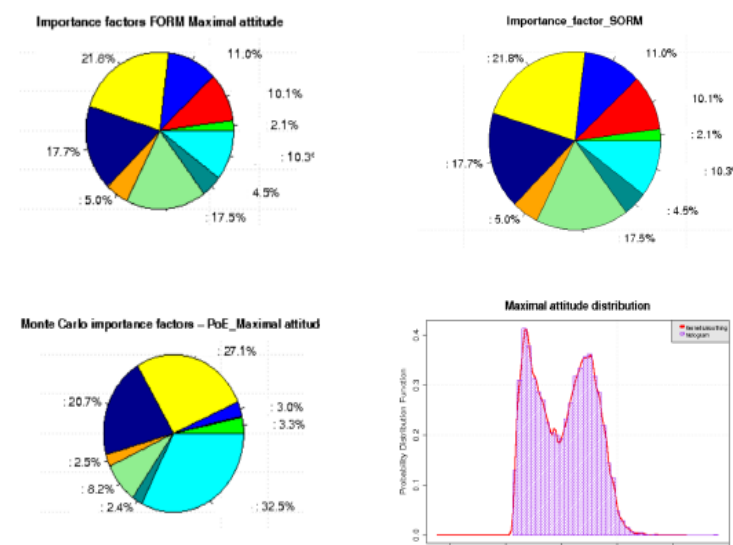


Figure: Sensitivity to the probability

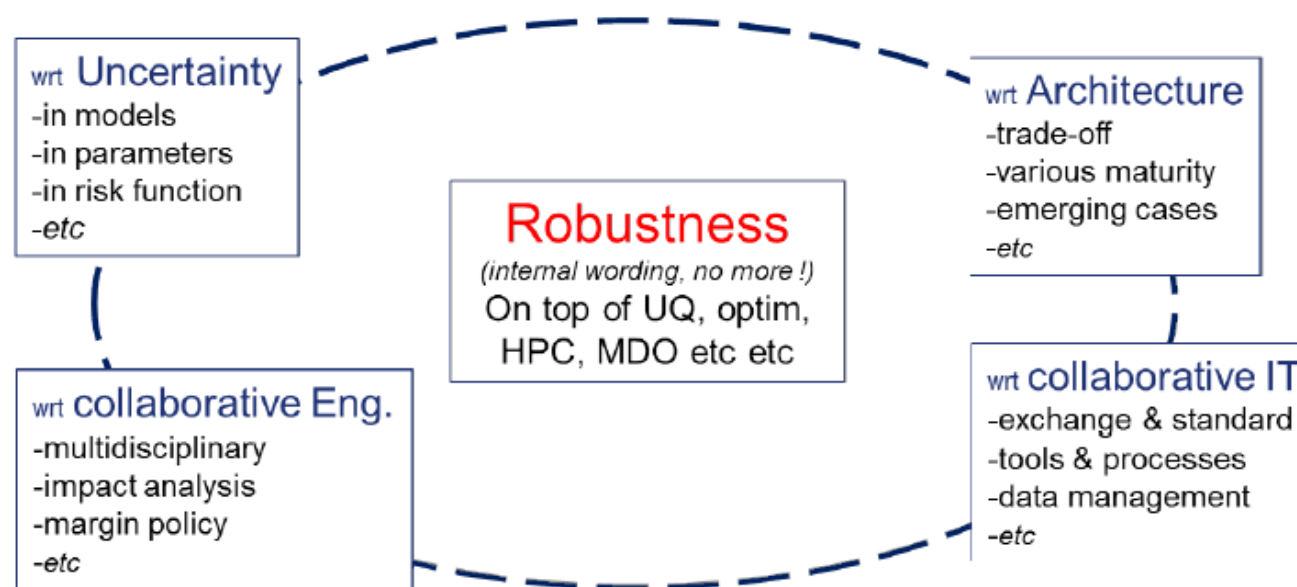
# UNCERTAINTY MANAGEMENT

## Next steps

- Integrate classical UQ techniques in the post analysis of optimization processes
  - Validation, tests & benchmarks
- Link with Robust Optimization capabilities to each scalability
- System view: Make the link with detailed design engineering & classical work breakdown structures organisations

# ROBUST OPTIMIZATION

## What do we mean by "robustness" within an industrial context ?



*It's not a pure matter of tool or math, neither an issue in data or model exchange; it's a pure collaborative challenge: wording, methodology, common understanding etc And each team to be at the right place to solve each bit of the set of difficulties 😊*



# ROBUST OPTIMIZATION

## Global Context



- Cost function  $J$  is derived mainly from "functional/system" consideration (mass, consumption, range of action, etc.)
- Constraints  $g$  are very often "complex physical simulation" (no analytical expression): temperature, aerodynamic coeff., displacement, etc.
- The interaction between the objective function  $J$  and constraints  $g$  induces couplings "physics-system" (e.g thermal regulation: system = air conditioning pack / physics = fluid behavior in the cabin)

**Margins are everywhere**

due to the way our products were designed. Value will be created by rigorously chasing them !

Optimization strategies also impact organisations !

# ROBUST OPTIMIZATION

## Global Context

- From a classical (parametrized) optimization problem ...

$$\min_{\mathbf{x}, \mathbf{g}(\mathbf{x}, \mathbf{u}) \leq 0} J(\mathbf{x}, \mathbf{u})$$

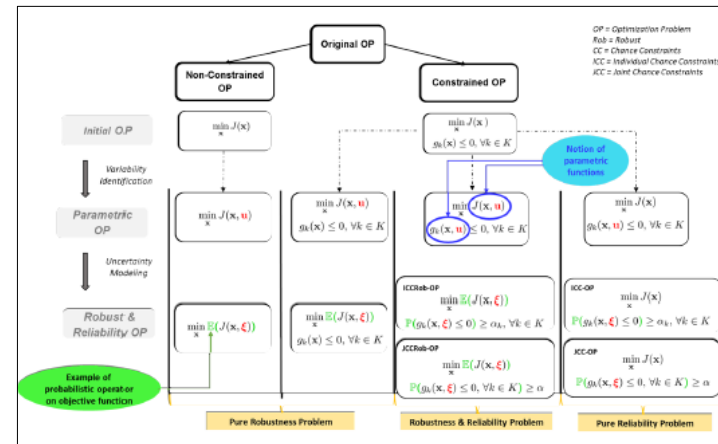
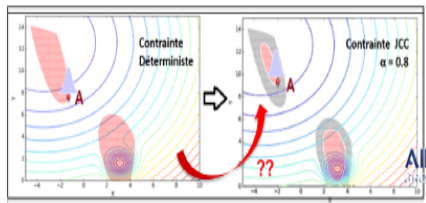
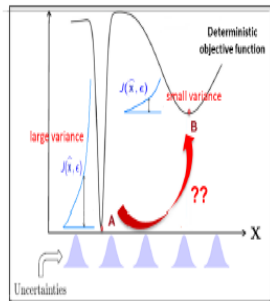
where  $\mathbf{u}$  is some vector of values used in the problem (often hidden!)

- how to take into account uncertainties on  $\mathbf{u}$  and/or on the design  $\mathbf{x}$  ?
- For simplicity, data  $\xi$  will aggregate all sources of uncertainties (on design, on environmental constants, etc.)
- $\xi$  is modelled as a random vector with distribution  $\mathbb{P}_\xi$
- In practice, the engineer solves a parametrized optimization problem

$$\min_{\mathbf{x}, \mathbf{g}(\mathbf{x}, \xi(\omega)) \leq 0} J(\mathbf{x}, \xi(\omega))$$

for some scenario  $\xi(\omega)$  of the uncertainties that he has fixed before

## Robust & Reliable Optimization

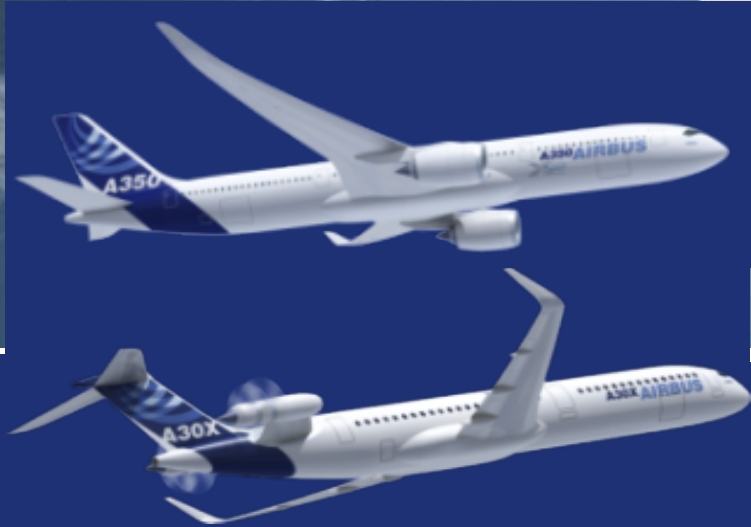


# MULTI DISCIPLINARY OPTIMIZATION

## Next steps

- **Understand** the Robust Optimization capabilities for a set of applicative problems
  - Validation, tests & benchmarks
  - Extension of physical analysis (low/high fidelity → adequacy)
- **Develop** the Robust Optimization capabilities to each scalability
  - Acoustics,
  - Thermics
  - System models (0D-1D)
- **Capitalize** in an open source software
- **System view**: Make the link with detailed design engineering & classical work breakdown structures organisations

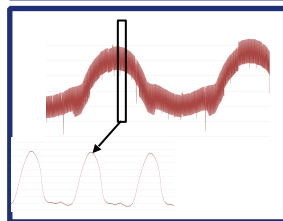
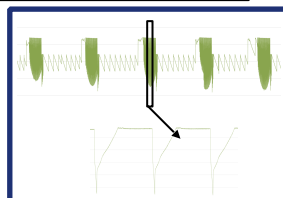
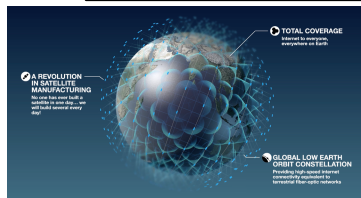
4



Perspectives

# NEW TOPICS: DATA ANALYTICS

## SATELLITE FLEET WATCH

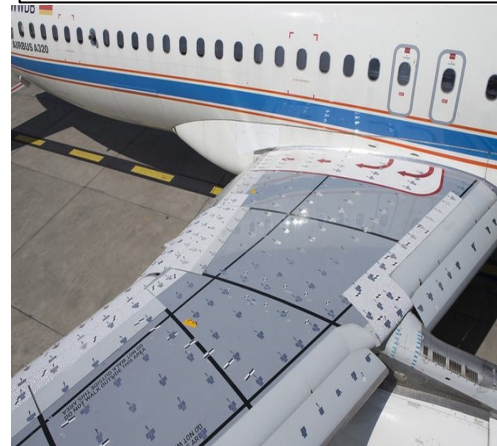


Phase	Phase	Etapes	Technique	Contexte	Cible	Méthode	Avantages	Quelques
Phase 1	Phase 2	Phase 3	Phase 4	Phase 5	Phase 6	Phase 7	Phase 8	Phase 9
Phase 1	Phase 2	Phase 3	Phase 4	Phase 5	Phase 6	Phase 7	Phase 8	Phase 9
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Phase 1	Phase 2	Phase 3	Phase 4	Phase 5	Phase 6	Phase 7	Phase 8	Phase 9
Phase 1	Phase 2	Phase 3	Phase 4	Phase 5	Phase 6	Phase 7	Phase 8	Phase 9

Operability of single satellite based on telemetry gathered at fleet level

Many sensors  
Year/month/day/min/sec datasets  
Active fleet of satellites

## FLIGHT-TEST DATA



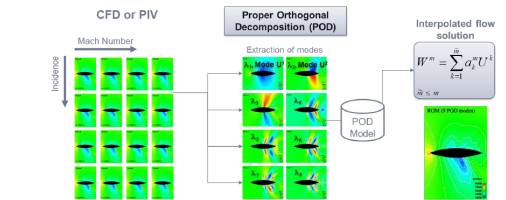
Flight-Test plan reduction  
Better maturity @ EIS

500 sensors  
10 physical parameters  
100 Flights

## SIMULATION CFD // MEASUREMENT PIV

Technical Approach 1/2

- CFD and PIV provide discrete solutions (snapshots) for different flow conditions (left picture)
- The result space is decompose into modes (middle picture)



- The reconstruction of any intermediate condition is possible (right picture)

Calibration & data mining in large simulation datasets



## SPECIFIC OPTIMIZATION PROBLEMS FOR SPECIFIC HARDWARE INFRASTRUCTURES



- Quantum Computing is emerging and seems to be very promising for specific optimization problems

## CONCLUSION

- Mathematical algorithms make the difference but this is not sufficient !
- Engineers are not used to build/model optimization problems and this is not only a numerical problem
- On-going research to embrace the Robust Multi Disciplinary Optimization vision
- New topics to arise in optimization to take advantage of future on-line learning capabilities of our platforms (Big Data, Quantum Computing)
- Communities to be built between Uncertainty Quantification (GDR MASCOT-NUM/SIAM UQ) & Optimization (You !)



**Thank you !**

For the invitation !  
For the disrupted schedule !  
For your questions !